

Finite Element Based LRFD Design of Bottomless Culverts



Presented By:

Craig Chatelain, P.E., AECOM

Ahilan Selladurai, P.E., AECOM



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AUTHORS

Dallas Forester, P.E., CALTRANS

Bob Fish, P.E., S.E., AECOM

Ahmad M Abdel-Karim, Ph.D., P.E., AECOM

Ahilan Selladurai, P.E., AECOM

ACKNOWLEDGEMENT



Department of Transportation, California

- ❖ **Shannon Post, Chief, Office of Design and Technical Services**
- ❖ **Roberto Lacalle, Chief, Office of Design and Technical Services**
- ❖ **Dallas Forester, Task manager**
- ❖ **K.K.Lin, Transportation Engineer**
- ❖ **Yu Song, Transportation Engineer**



CONTECH Bridge Solutions Inc.

- ❖ **Michael G. Carfagno, Vice President – Engineering Development**
- ❖ **Mark A. Taylor, Area Technical Director, California**
- ❖ **Gina Spears, Region Manager, San Diego, California**
- ❖ **Michael G. Katona, Consultant**



WBES – 2011 COMMITTY

Finite Element Based LRFD Design of Bottomless Culverts



Presented By:

PART – I

Craig Chatelain, P.E.

Introduction

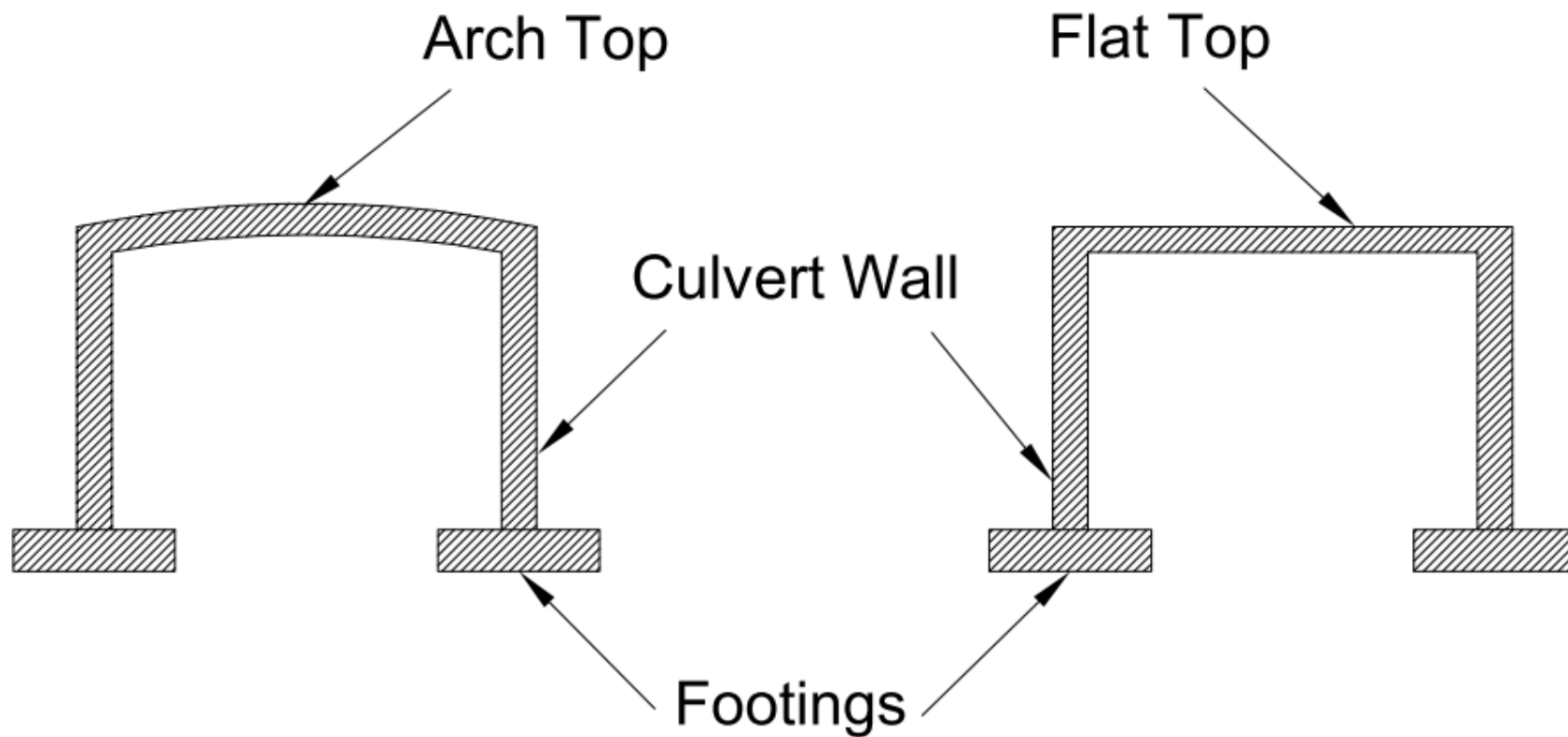
A. Description

- Definition
- Example Applications

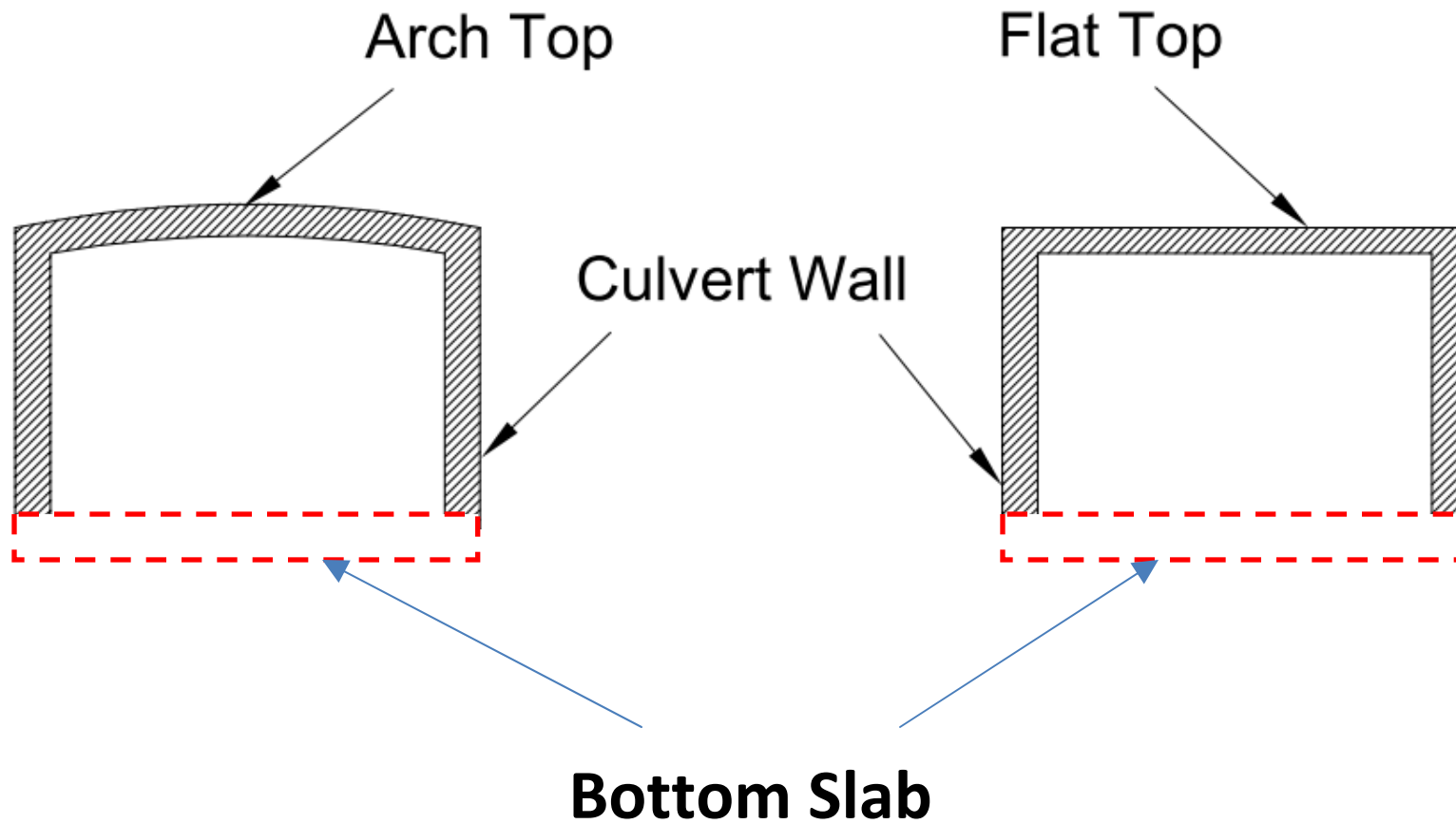
B. Design Methodology

C. Project Objectives

Definition



Definition



Example Applications

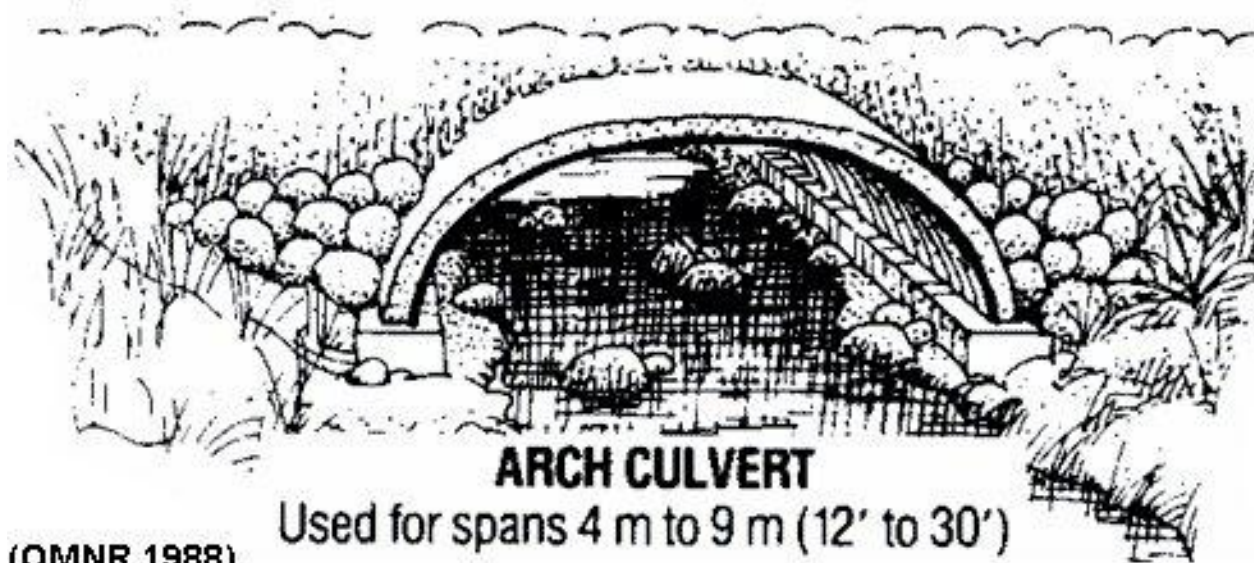


Concrete



Metal (Aluminum / Steel)

Green Applications



ARCH CULVERT

Used for spans 4 m to 9 m (12' to 30')

(OMNR 1988)

Green Applications – Fish Passages



Green Applications – Fish Passages



Green Applications – Fish Passages



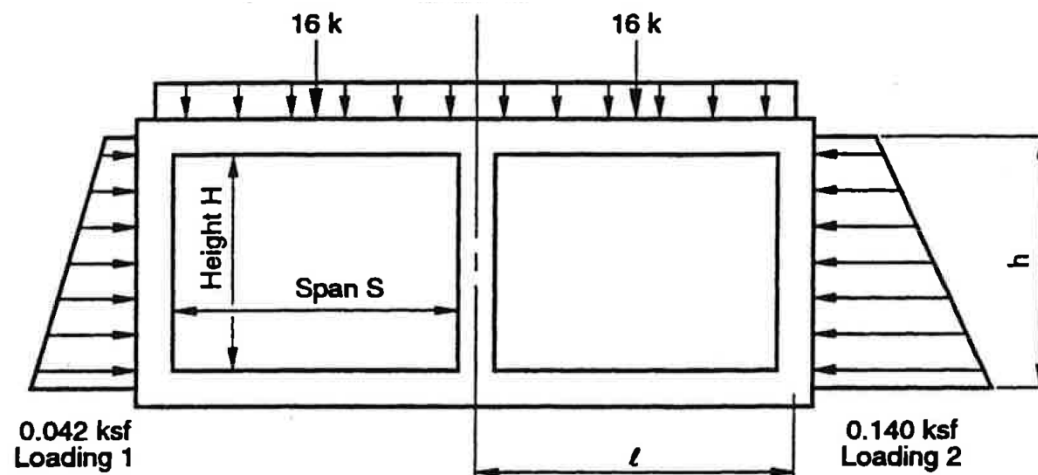
Green Applications – Animal Crossings



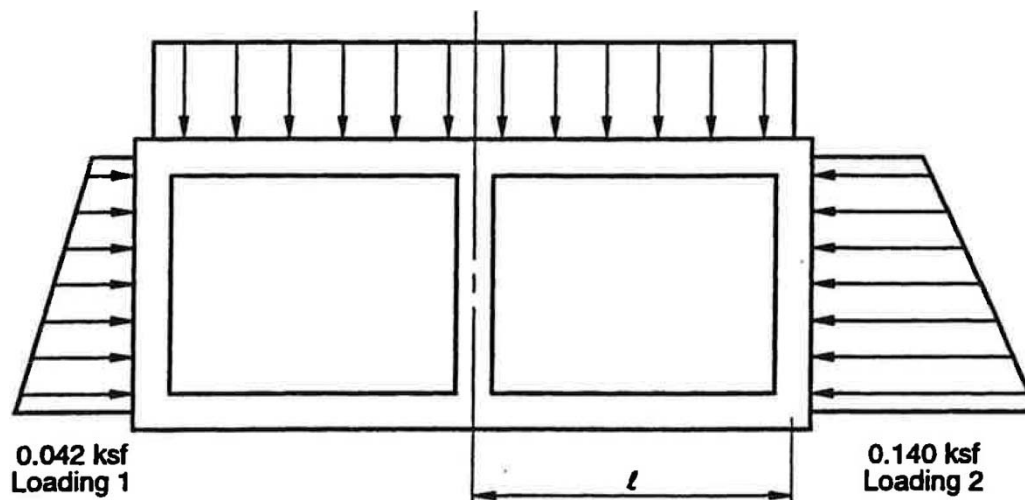
B. Design Methodology

- Traditional
- Detailed (FEM)
- Transition to LRFD

Traditional Methods- Caltrans Pressure Envelopes

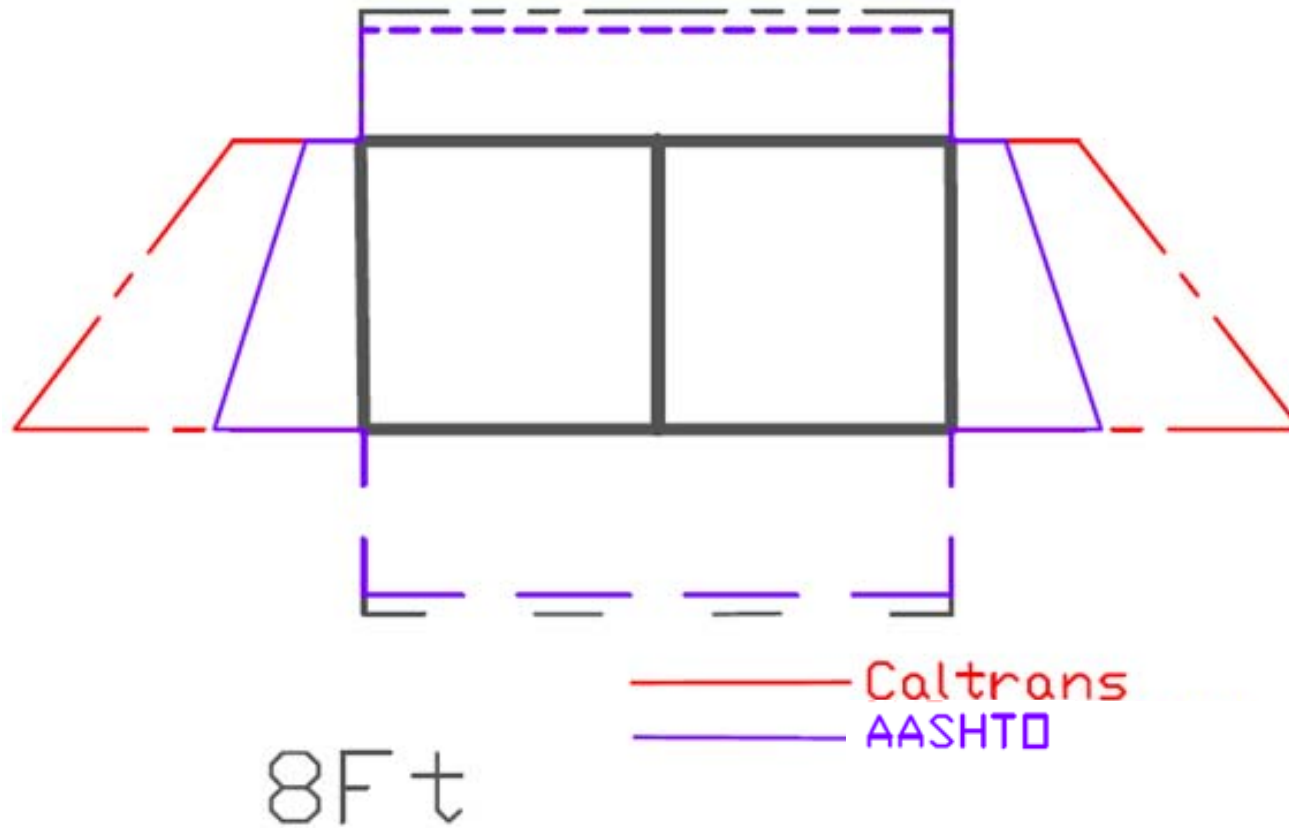


Condition 1: 2' Cover



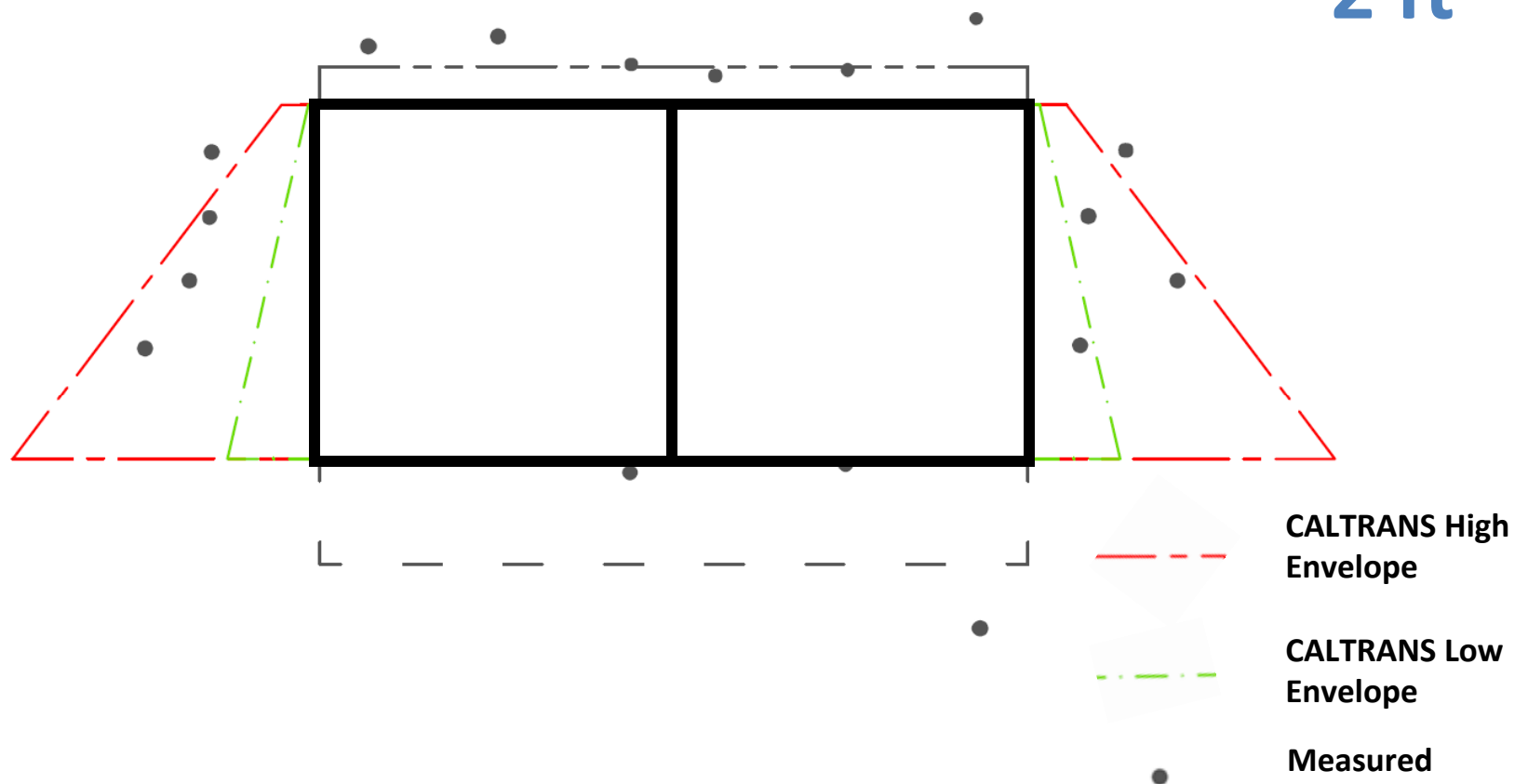
Condition 2: 10' Cover

Caltrans vs AASHTO

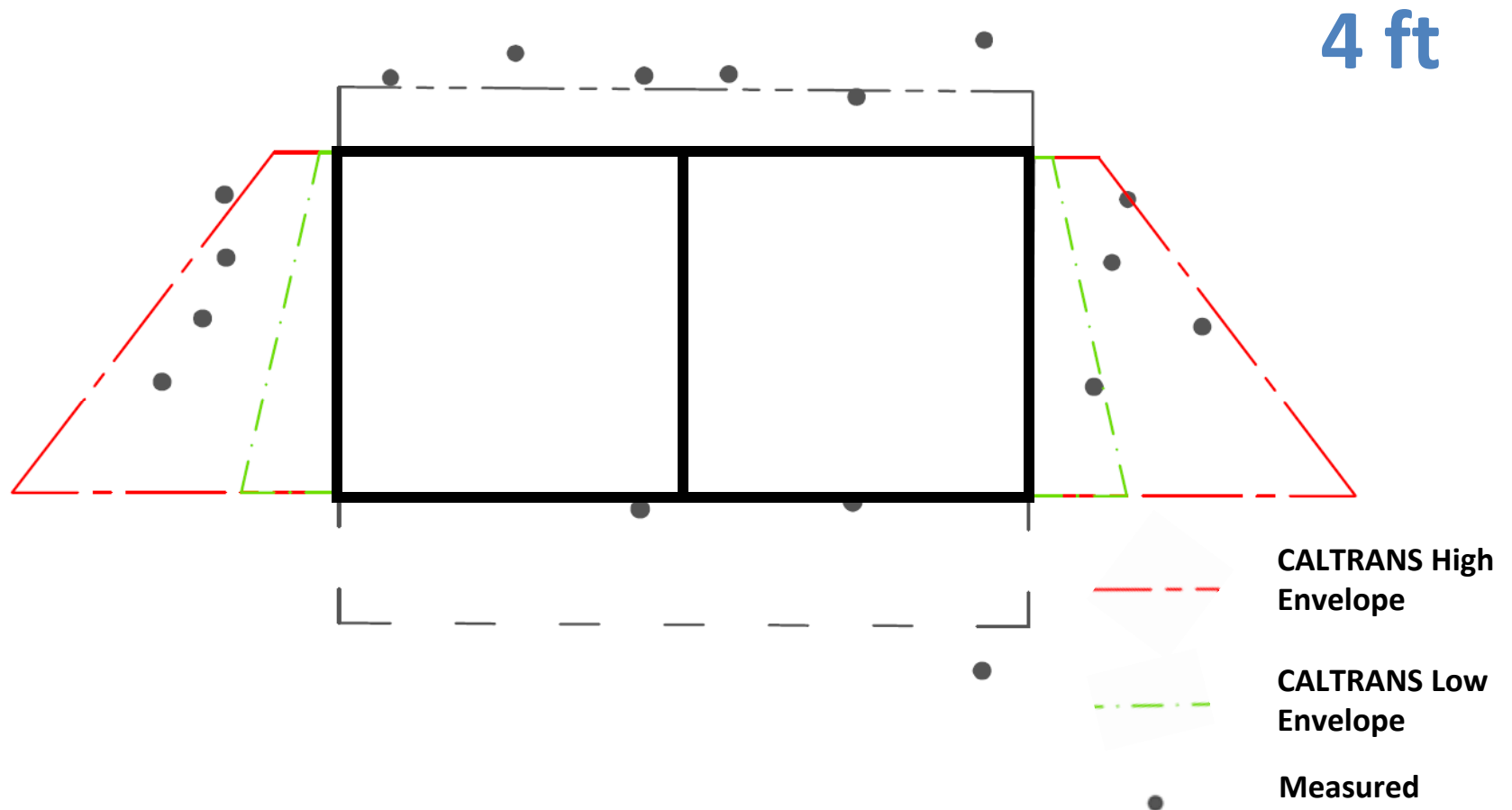


1989 Full-Scale Testing (University of Nebraska)

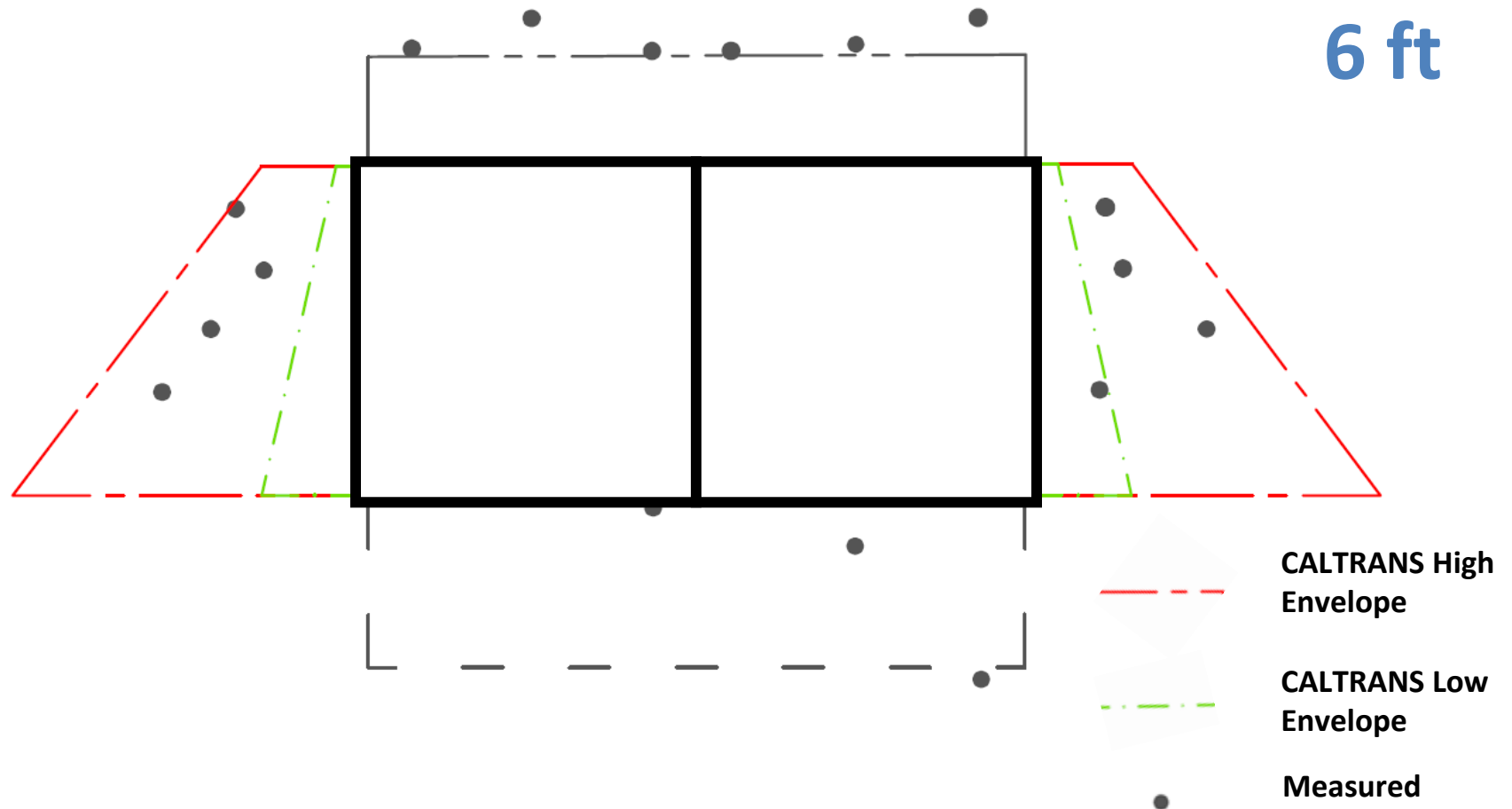
2 ft



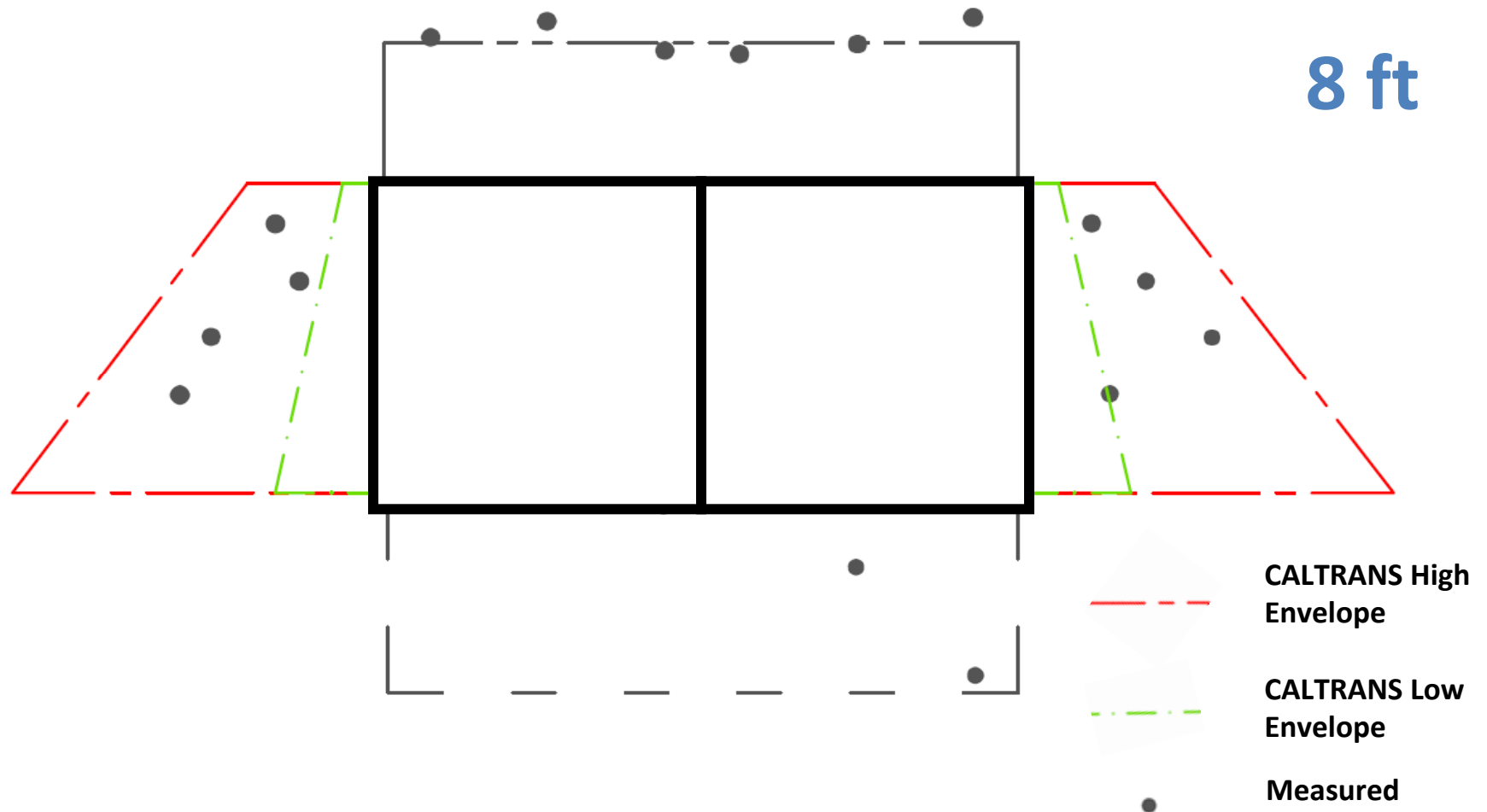
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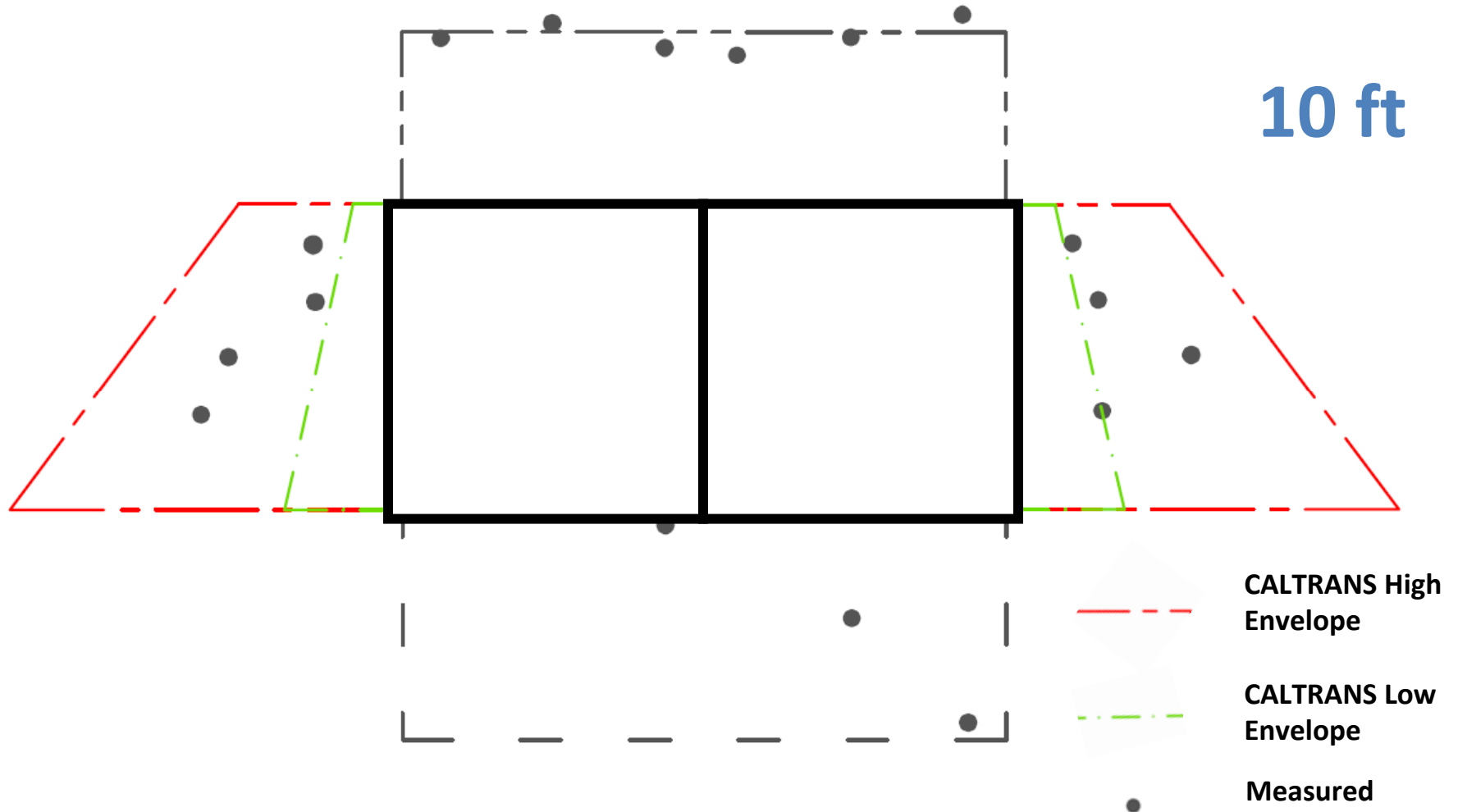


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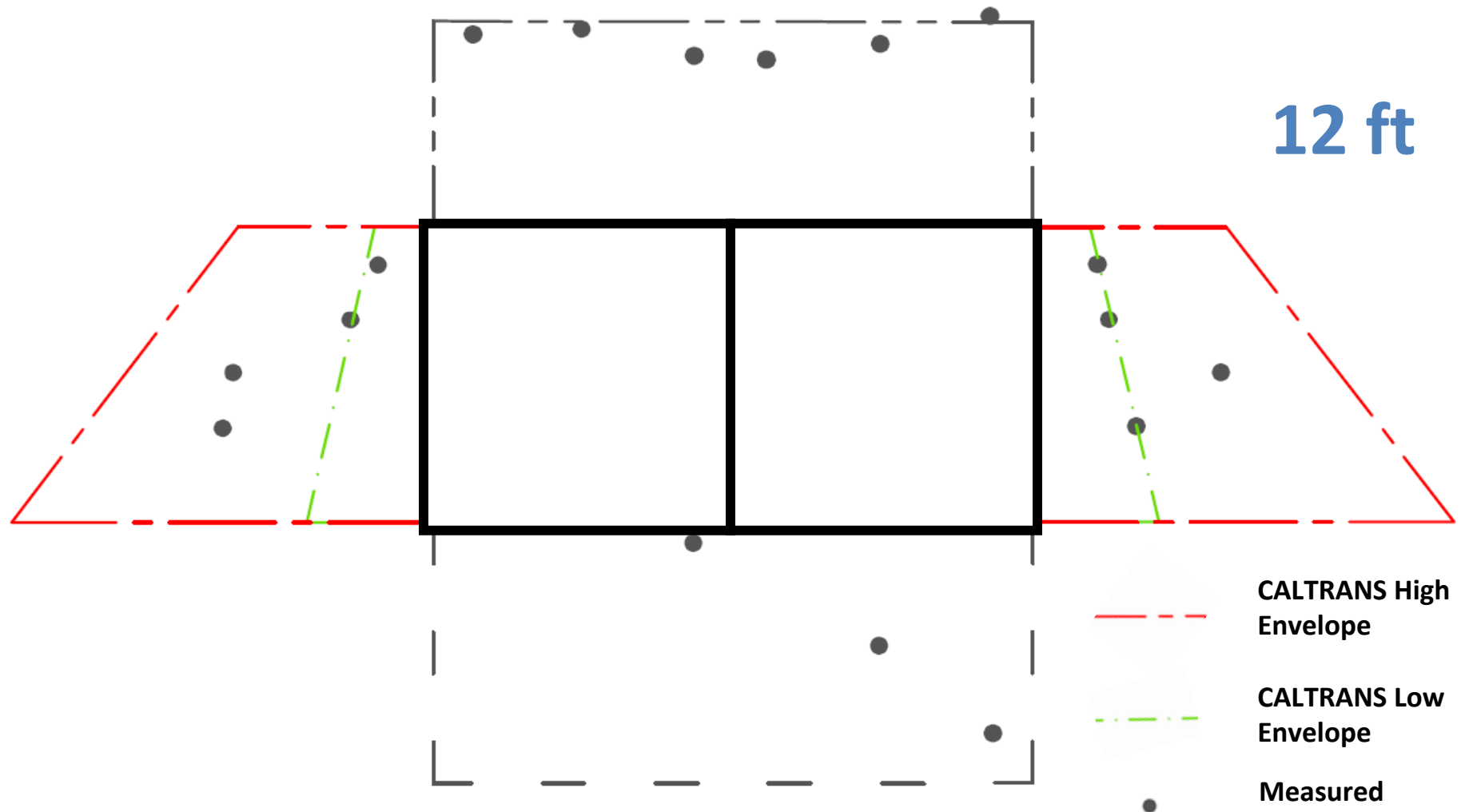


1989 Full-Scale Testing (University of Nebraska)

10 ft

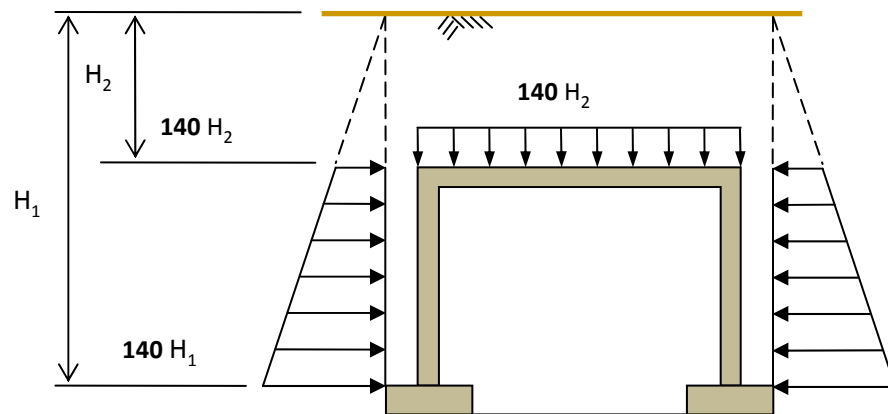


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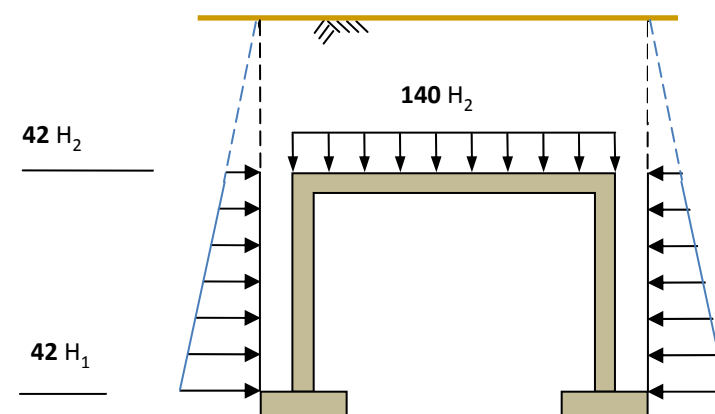


Caltrans Earth Pressure Envelopes

CALTRANS MAXIMUM ENVELOPE

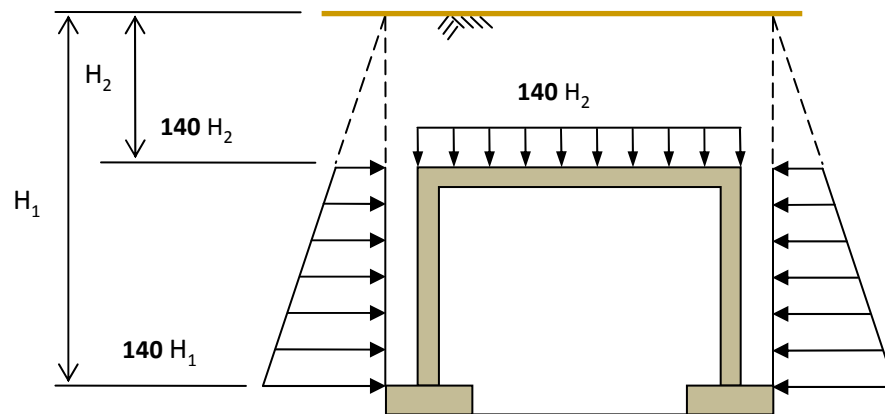


CALTRANS MINIMUM ENVELOPE

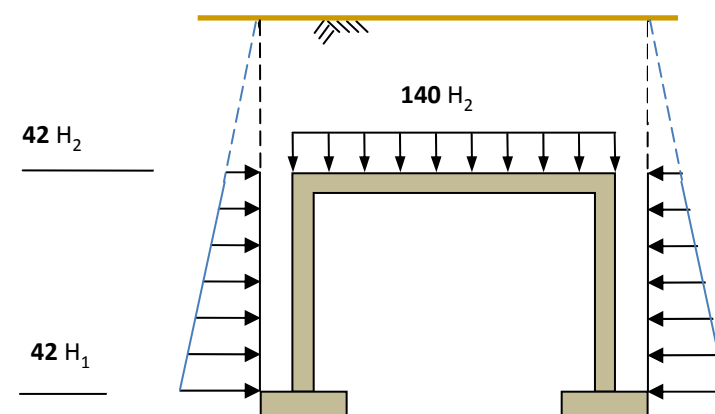


Caltrans Earth Pressure Envelopes

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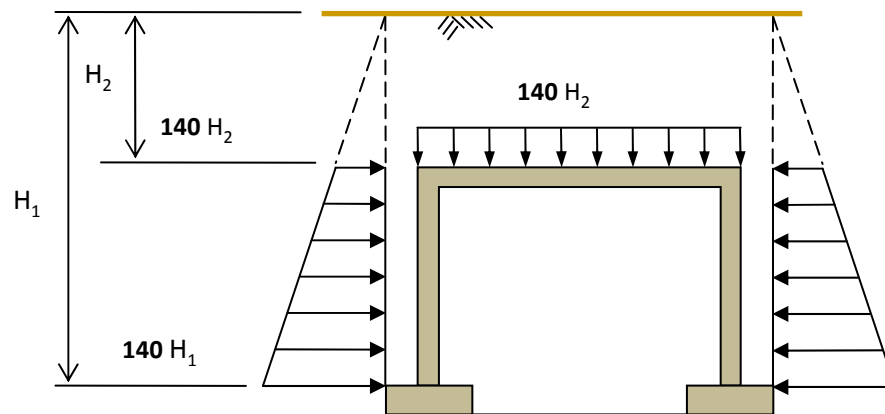
CALTRANS MINIMUM ENVELOPE



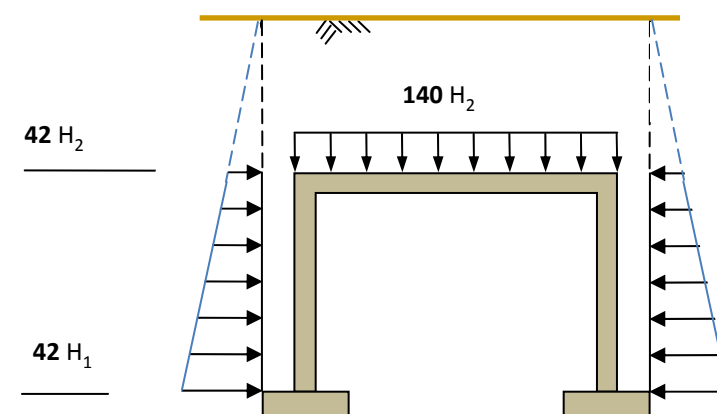
- Have been successfully used for nearly 30 years!

Caltrans Earth Pressure Envelopes

CALTRANS MAXIMUM ENVELOPE

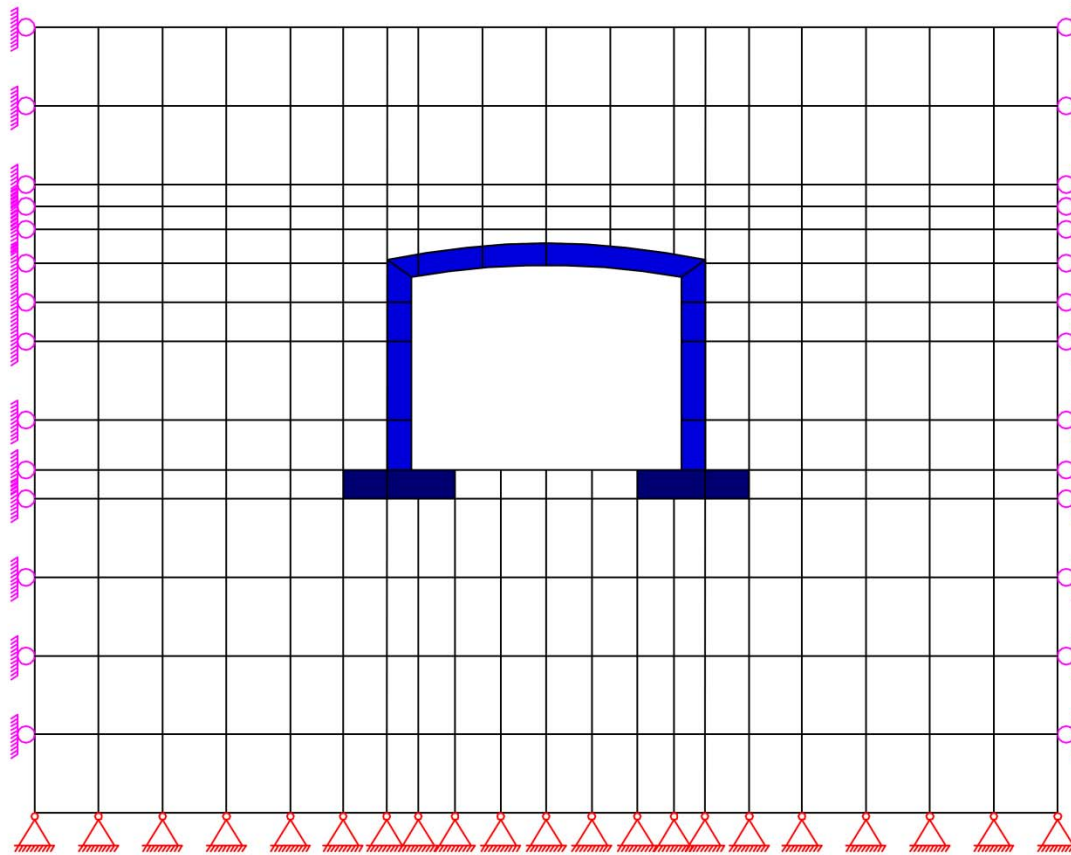


CALTRANS MINIMUM ENVELOPE



- Have been successfully used for nearly 30 years!
- Have a great deal of credibility

Detailed Methods- Finite Element Method (FEM)



FE Mesh

Detailed Methods- Finite Element Method (FEM)

Advantages of FEM:

- Accounts for Soil-Structure Interaction
- Accounts for Variability of Materials
- Takes into Account Material Non-linearity
- Detailed modeling of Live Load Effects
- Fast!

Departure from Traditional- Considerations:

- Precedence
- Designer's Confidence
- Other (Seismic Design)

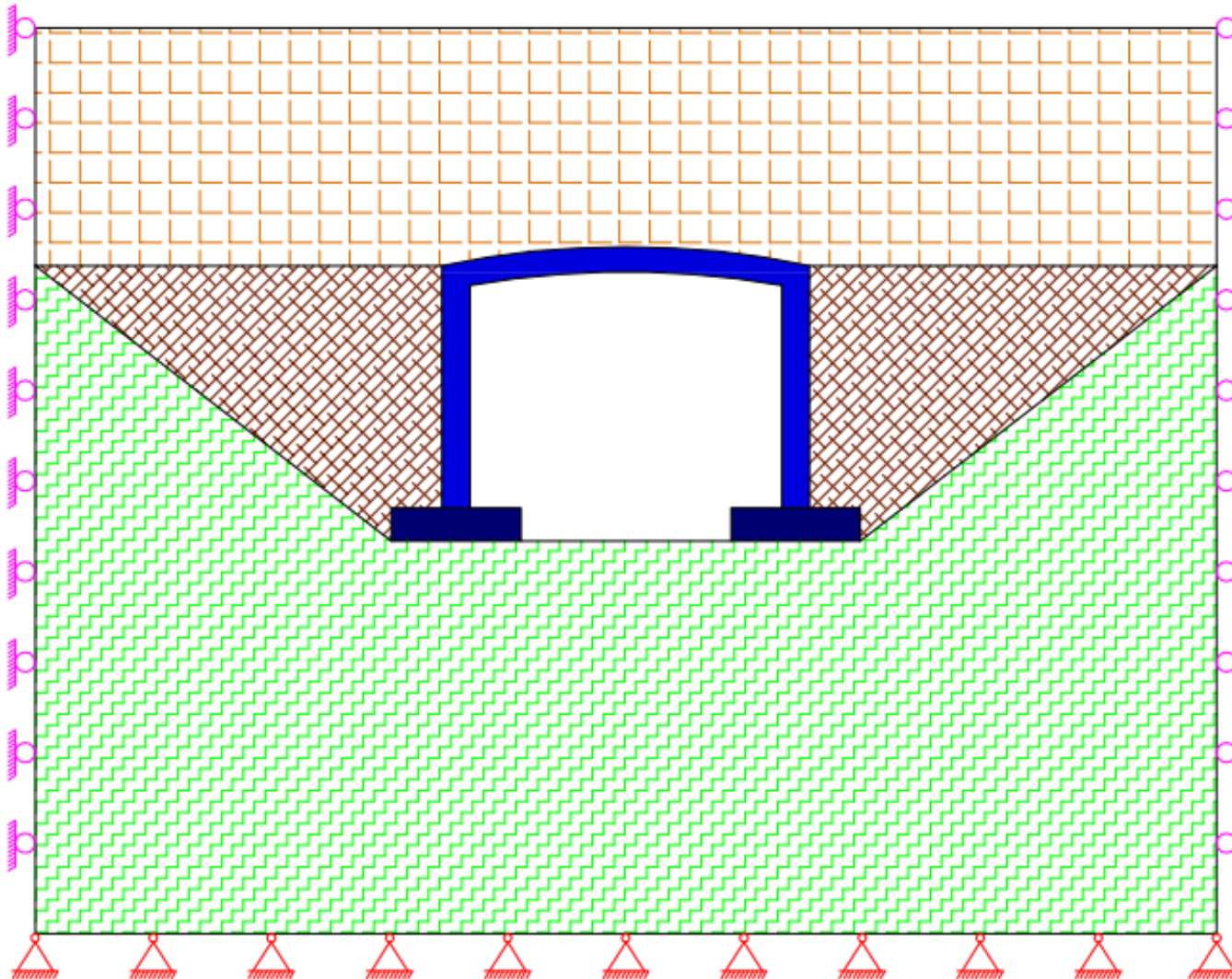
LRFD Adaptation- *A Calibration Process:*

- Obtain similar level of confidence to the Traditional Method
- Fine-tune the modeling parameters & methodology to meet LRFD requirements

C. Project Objectives

- Review Submittals for specific Culverts
- Verify Design Methodology & Conclusions
- Develop Recommendations for Streamlining the Review Process to Expedite Approval

SUBMITTAL REVIEW



General:

- 20' Max Span
- No Seismic

Review Problem:

- 16 ft Span
- 10 ft Rise
- 20 ft Max Fill

Finite Element Based LRFD Design of Bottomless Culverts

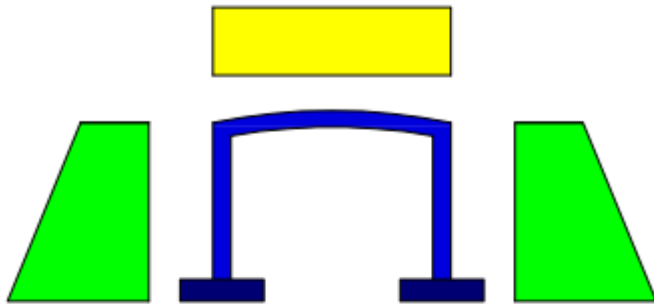


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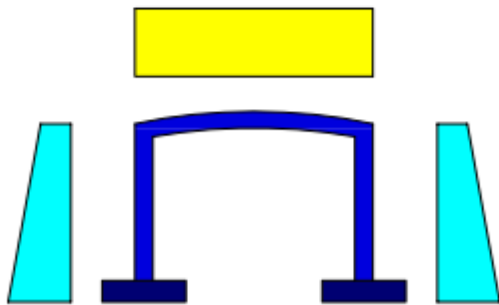
PART – II

Ahilan Selladurai, P.E.

High Envelope

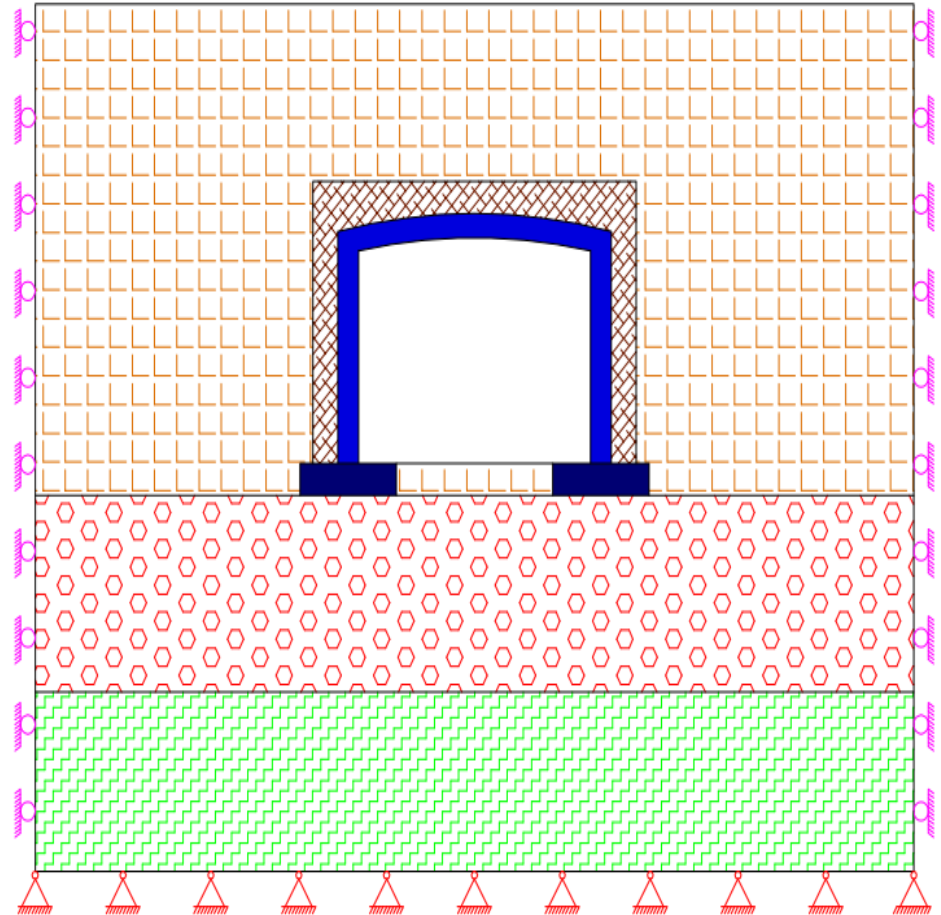


Low Envelope



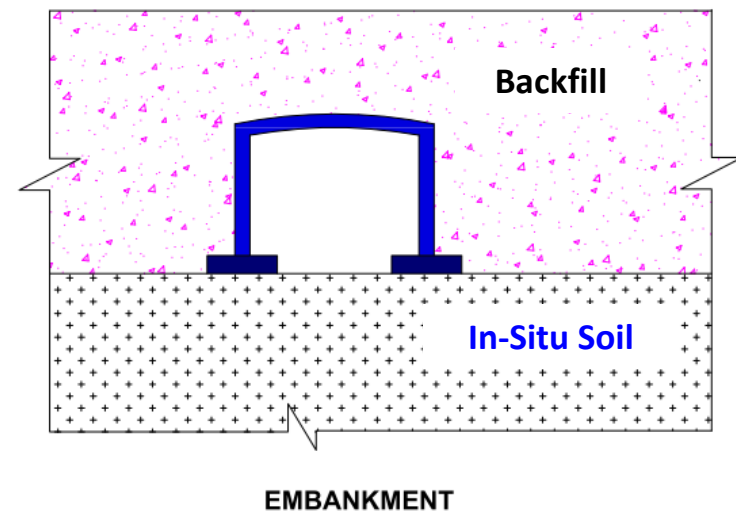
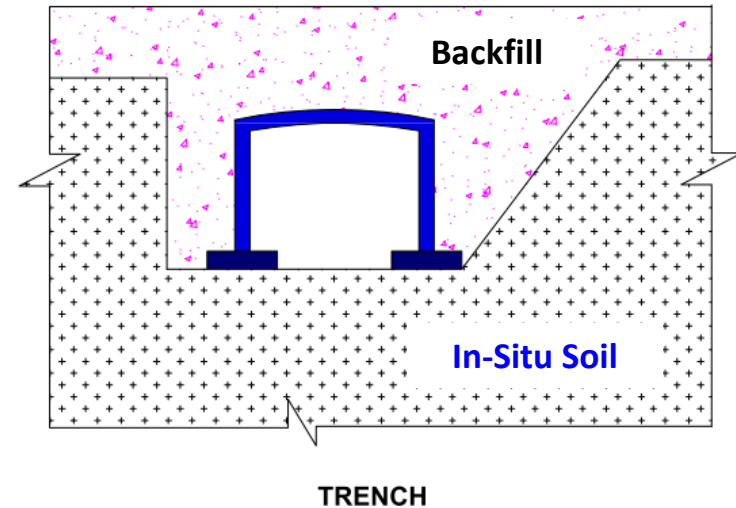
CALTRANS CONVENTIONAL

Embankment Condition

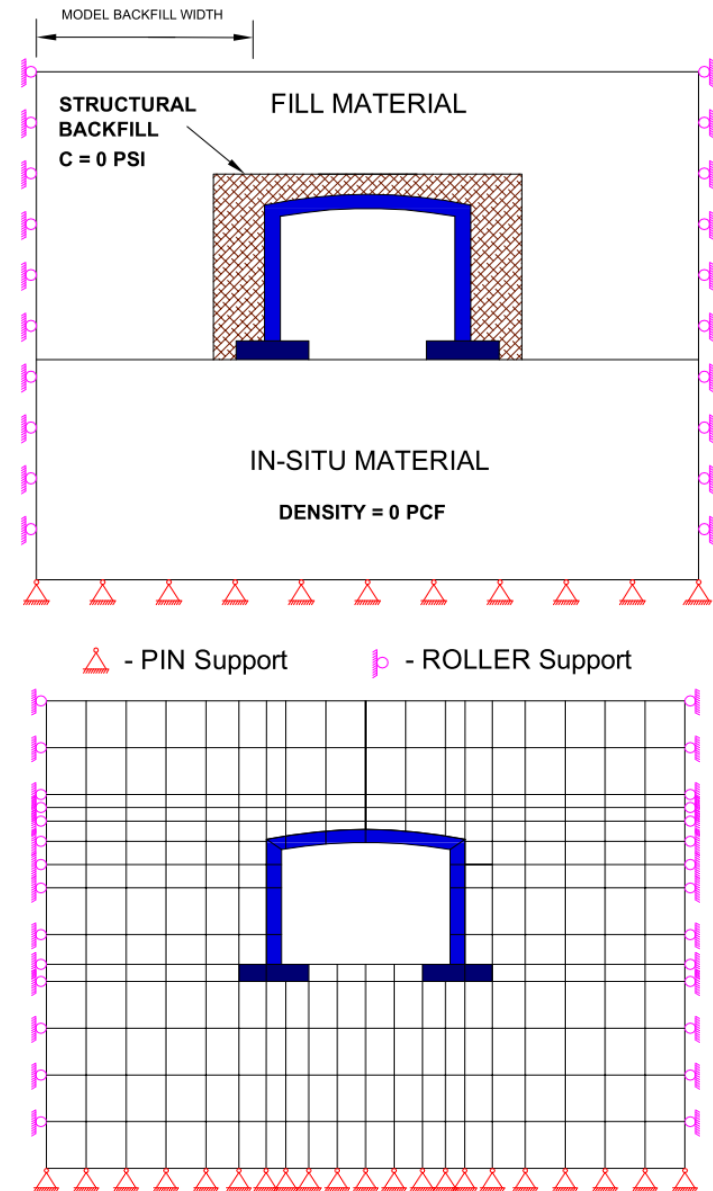


DETAIL FINITE ELEMENT MODEL

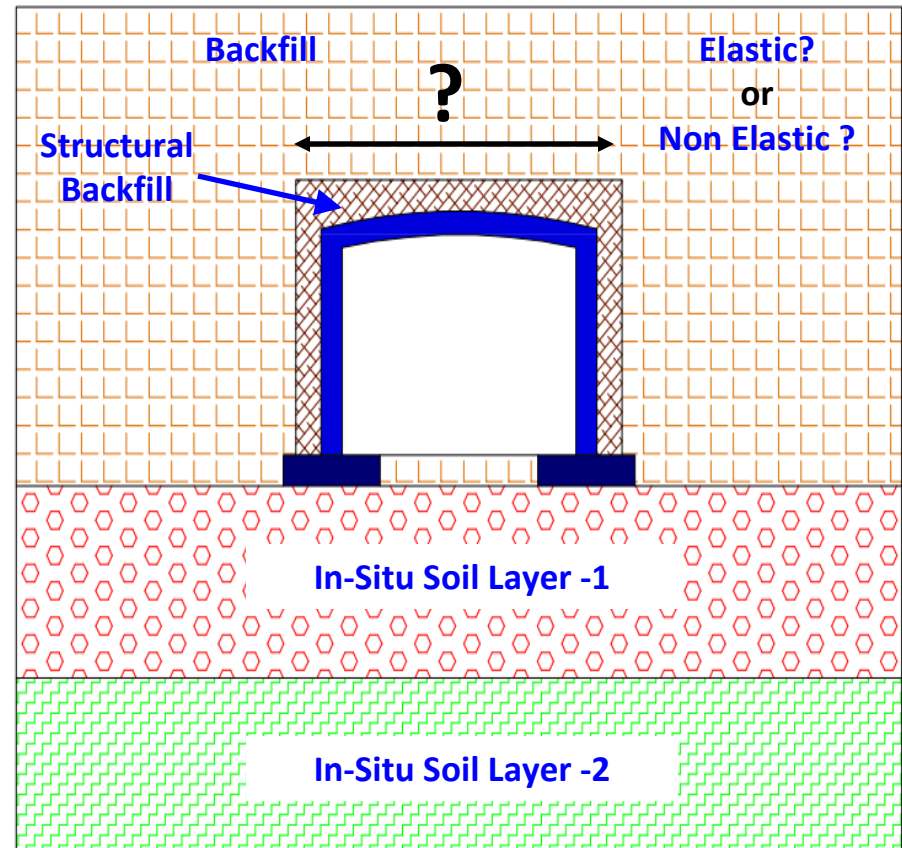
- **Installation condition**
- Finite Element Model
- Soil Types & Limits
- Soil Properties
- Interface Elements
- Live Load Analysis
- Load Factors & Combinations
- Design Recommendations



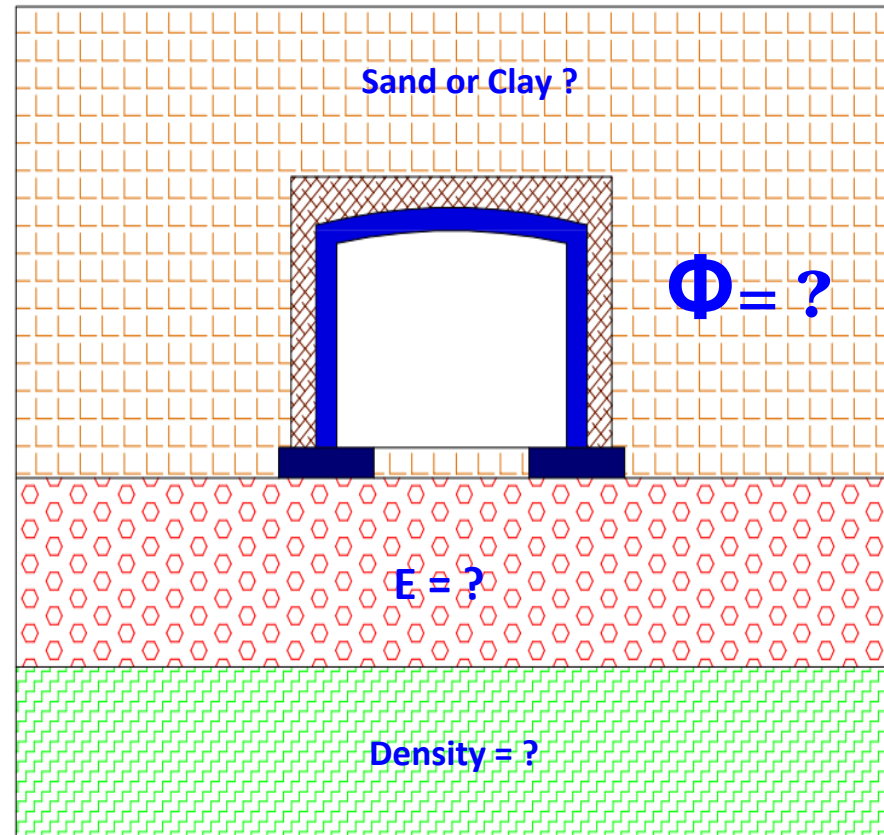
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- Installation condition
- Finite Element Model
- **Soil Types & Limits**
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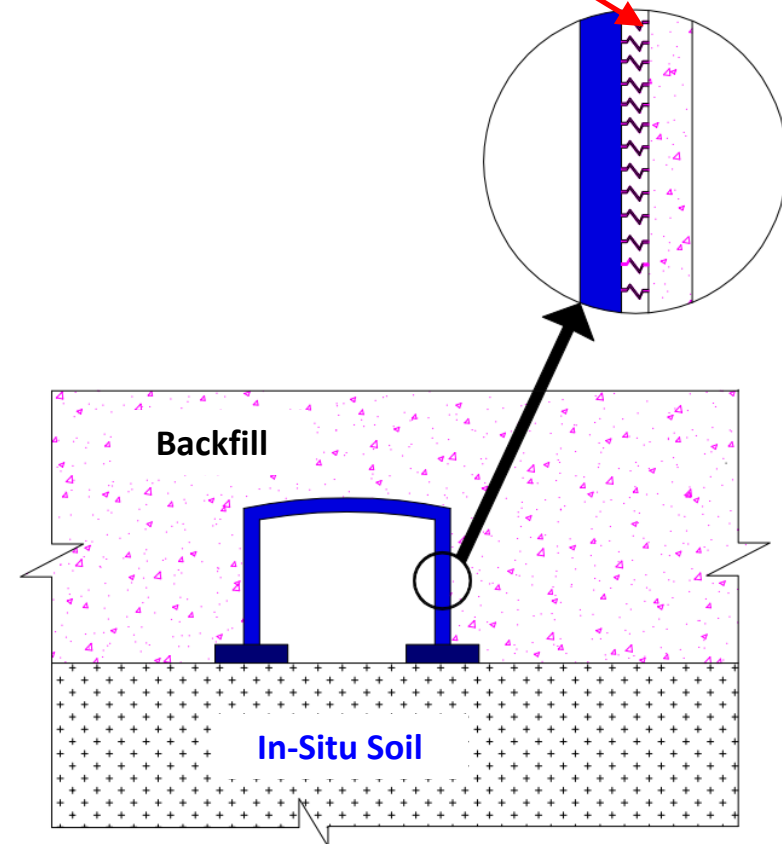


- Installation condition
- Finite Element Model
- Soil Types & Limits
- **Soil Properties**
- Interface Elements
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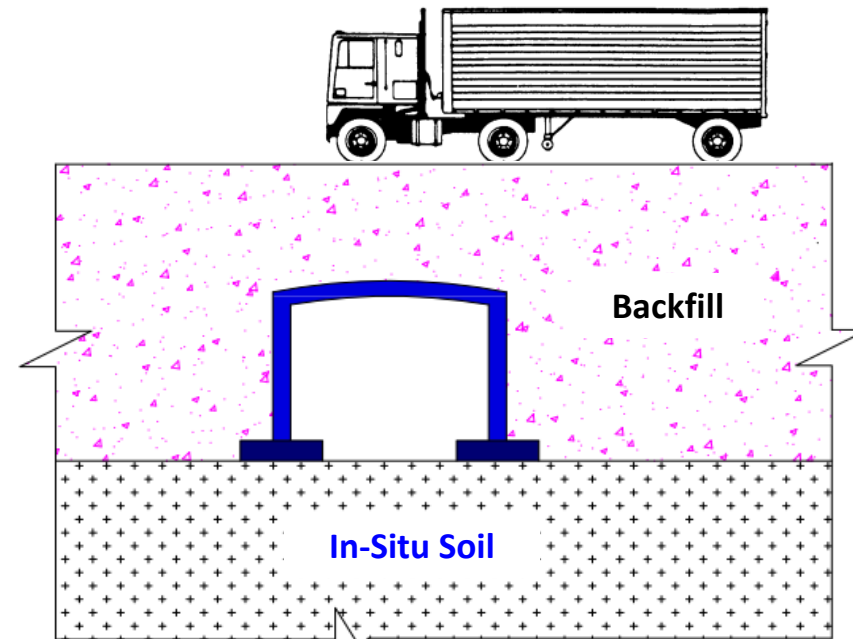


- Installation condition
- Finite Element Model
- Soil Types & Limits
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- **Interface Elements**
- Live Load Analysis
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**Interface
Elements ?**



- Installation condition
- Finite Element Model
- Soil Types & Limits
- Soil Properties
- Interface Elements
- **Live Load Analysis**
- Load Factors & Combinations
- Design Recommendations



REVIEW PROCESS

- Installation condition
- Finite Element Model
- Soil Types & Limits
- Soil Properties
- Interface Elements
- Live Load Analysis
- **Load Factors & Combinations**
- Design Recommendations

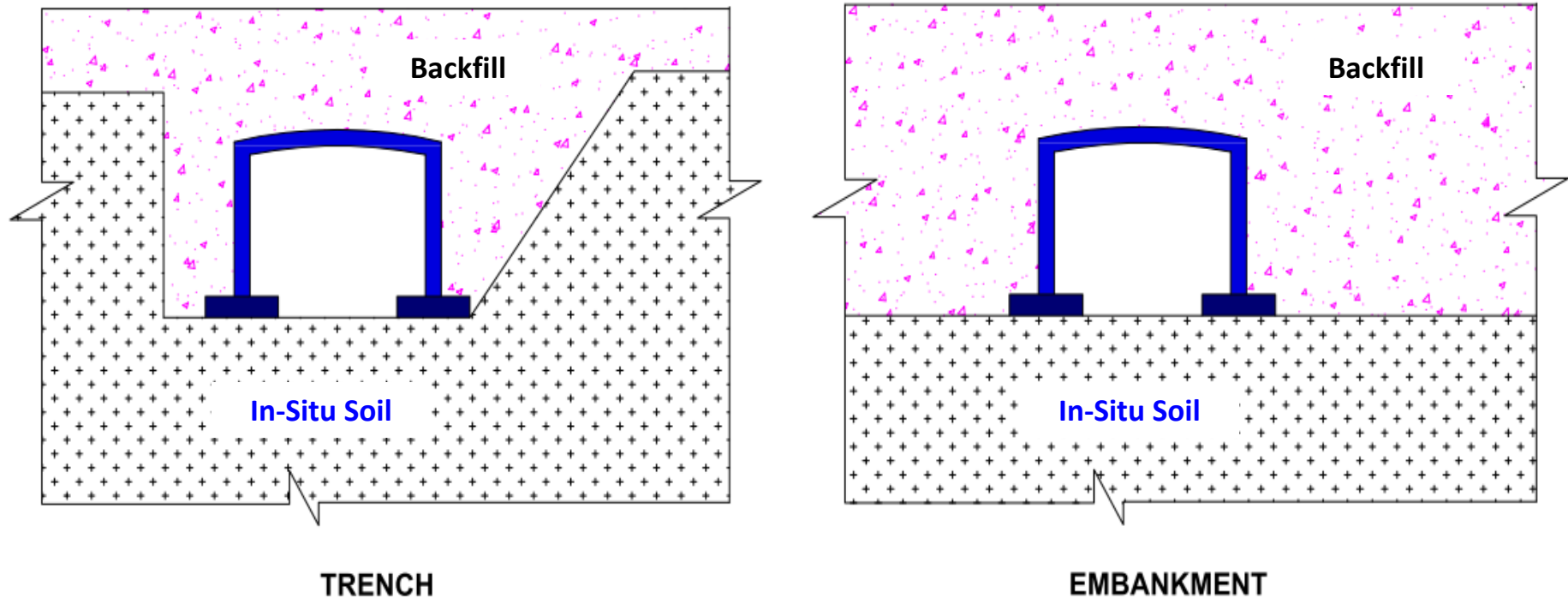
Table 3.4.1-1—Load Combinations and Load Factors

Load Combination Limit State	DC DD DW EH EV ES EL PS CR SH	LL IM CE BR PL LS	WA	WS	WL
Strength I (unless noted)	γ_p	1.75	1.00	—	—
Strength II	γ_p	1.35	1.00	1.40	—
Strength III	γ_p	—	1.00	—	—
Strength IV	γ_p	1.35	1.00	0.40	1.0
Strength V	γ_p	γ_{EQ}	1.00	—	—
Extreme Event I	γ_p	0.50	1.00	—	—
Extreme					

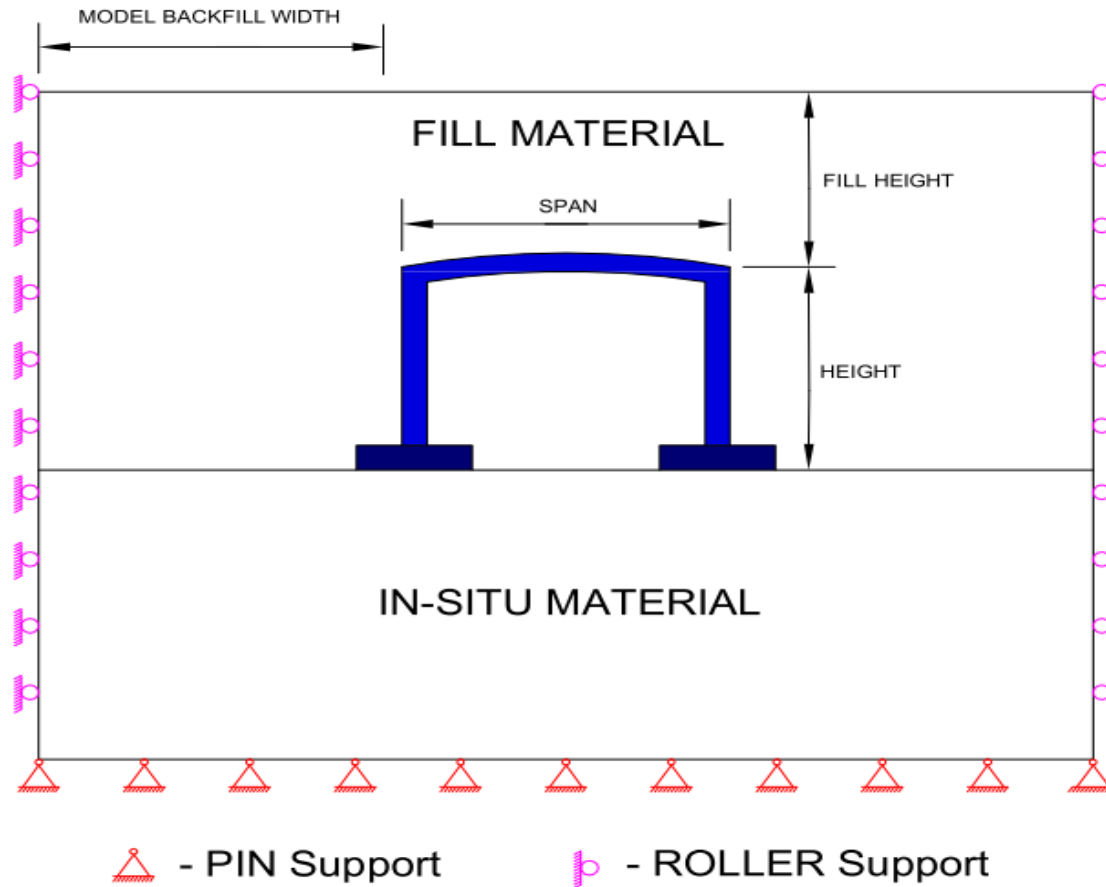
- Installation condition
- Finite Element Model
- Soil Types & Limits
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- **Design Recommendations**



- **Two types of Installation Conditions: Trench & Embankment Conditions**
- **Embankment Installation is Critical compared to Trench Installation.**

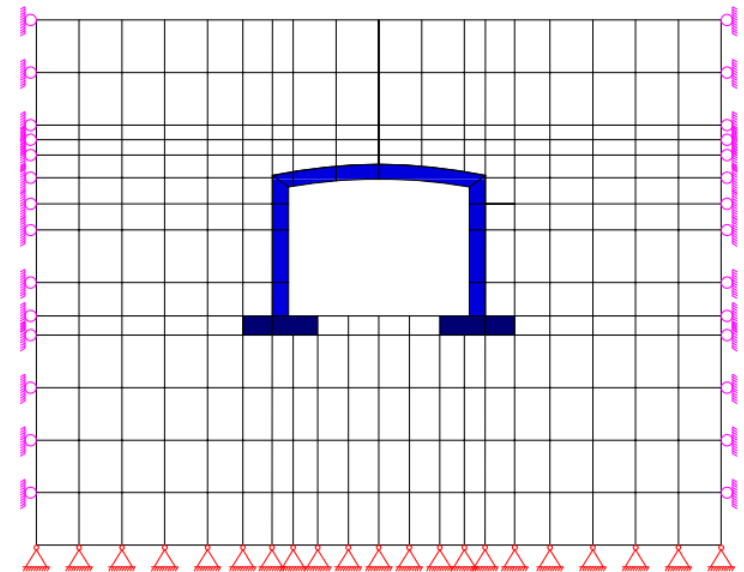


FINITE ELEMENT MODEL



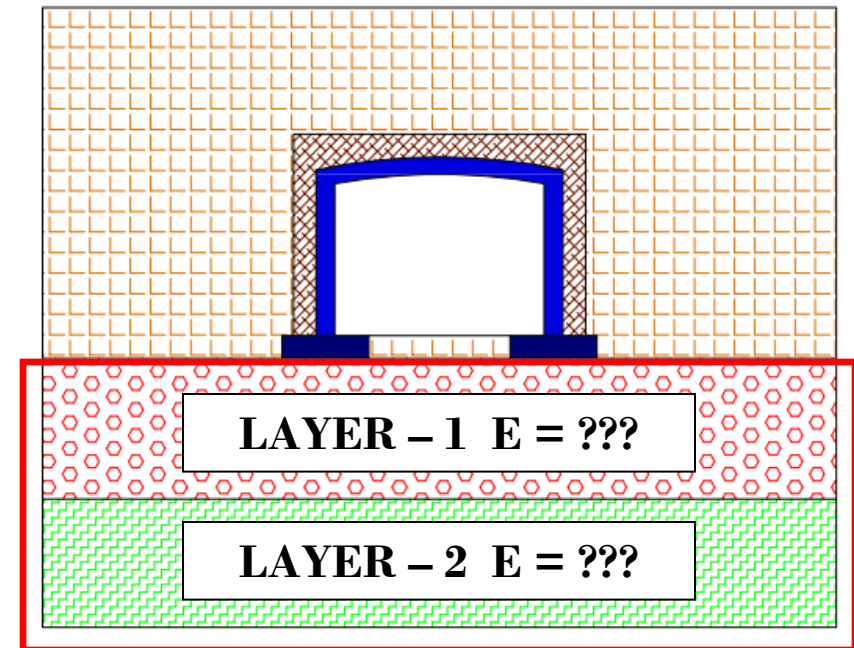
SUPPOTS CONDITION


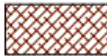
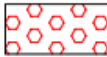
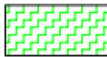


FE MESH



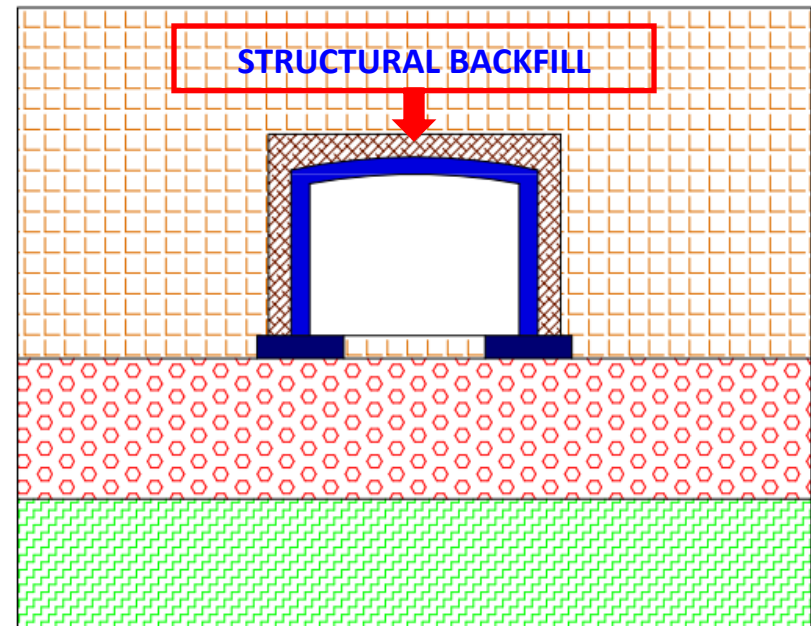
SOIL TYPES AND LIMITS



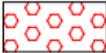



- **Bottom in-situ soil is typically divided one or two layers based on soil properties.**
- **Layer -1: Non linear if compacted soil layer.**
- **Width and fill height of structural backfill around the culvert significantly affect results.**
- **Other fill Soil may be assumed as linear elastic soil if there is no site specific soil information.**



-  - Linear Elastic Soil
-  - Duncan Selig Soil
-  - Linear Elastic Soil
-  - Linear Elastic Soil
-  - Linear Elastic Concrete
-  - Concrete Beam Elements

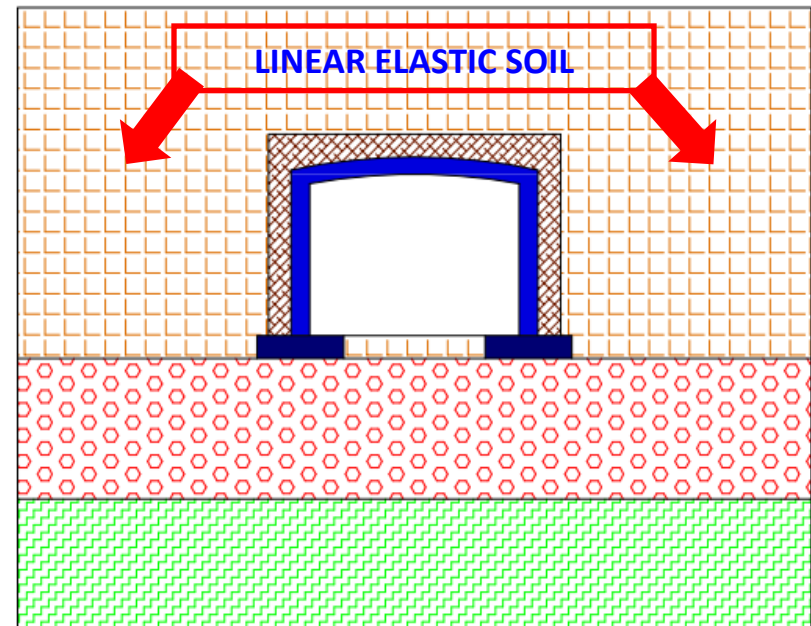
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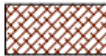
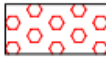
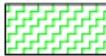




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SOIL TYPES AND LIMITS

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SOIL PROPERTIES

**TABLE 4.4.7.2.2A Elastic Constants of Various Soils
Modified after U.S. Department of the Navy (1982) and Bowles (1982)**

Typical Range of Values			Estimating E_s From $N^{(1)}$	
Soil Type	Young's Modulus, E_s (ksf)	Poisson's Ratio, ν (dim)	Soil Type	E_s (ksf)
Clay:				
Soft sensitive	50-300	0.4-0.5 (undrained)	Silts, sandy silts, slightly cohesive mixtures Clean fine to medium sands and slightly silty sands Coarse sands and sands with little gravel Sandy gravel and gravels	$8N_1^{(2)}$ $24N_1$
Medium stiff to stiff	300-1,000			
Very stiff	1,000-2,000			
Loess	300-1,200			
Silt	40-400	0.3-0.35		
Fine sand:			Estimating E_s From $s_u^{(3)}$	
Loose	160-240	0.25	Soft sensitive clay	$400s_u-1,000s_u$
Medium dense	240-400		Medium stiff to stiff clay	$1,500s_u-2,400s_u$
Dense	400-600		Very stiff clay	$3,000s_u-4,000s_u$
Sand:			Estimating E_s From $q_c^{(4)}$	
Loose	200-600	0.2-0.35	Sandy soils	$4q_c$
Medium dense	600-1,000	0.3-0.4		
Dense	1,000-1,600			
Gravel:				
Loose	600-1,600	0.2-0.35		
Medium dense	1,600-2,000	0.3-0.4		
Dense	2,000-4,000			

(1) N = Standard Penetration Test (SPT) resistance.
(2) N_1 = SPT corrected for depth.
(3) s_u = Undrained shear strength (ksf).
(4) q_c = Cone penetration resistance (ksf).

Ref: Caltrans Bridge Design Specifications, Nov 2003

SOIL TYPES & PROPERTIES

**TABLE 4.4.7.2.2A Elastic Constants of Various Soils
Modified after U.S. Department of the Navy (1982) and Bowles (1982)**

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Soil Type	Young's Modulus, E_s (ksf)	Poisson's Ratio, ν (dim)	Soil Type	E_s (ksf)
Clay:				
Soft sensitive			Very silty, slightly	$8N_1^{(2)}$
Medium stiff			clay mixtures	
to stiff			fine to medium sands	$14N_1$
Very stiff			slightly silty sands	
			sands and sands with	$20N_1$
			gravel	
			gravel and gravels	$24N_1$
Loess				
Silt	40-400	0.3-0.35		
Fine sand:				
Loose	160-240			
Medium dense	240-400	0.25		
Dense	400-600			
Sand:				
Loose	200-600	0.2-0.35		
Medium dense	600-1,000			
Dense	1,000-1,600	0.3-0.4		
Gravel:				
Loose	600-1,600	0.2-0.35		
Medium dense	1,600-2,000			
Dense	2,000-4,000	0.3-0.4		

Estimating E_s From s_u ⁽³⁾	
Soft sensitive clay	$400s_u - 1,000s_u$
Medium stiff to stiff clay	$1,500s_u - 2,400s_u$
Very stiff clay	$3,000s_u - 4,000s_u$

Estimating E_s From q_c ⁽⁴⁾	
Sandy soils	$4q_c$

Sand:
Loose: E= 200 – 600 ksf
Medium Dense: E= 600 – 1000 ksf
Dense: E= 1000 – 1600 ksf

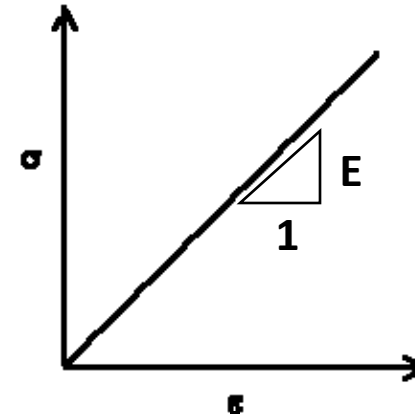
Sand:
Loose 200-600
Medium dense 600-1,000
Dense 1,000-1,600

(1) N = Standard Penetration Test (SPT) resistance.
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Ref: Caltrans Bridge Design Specifications, Nov 2003

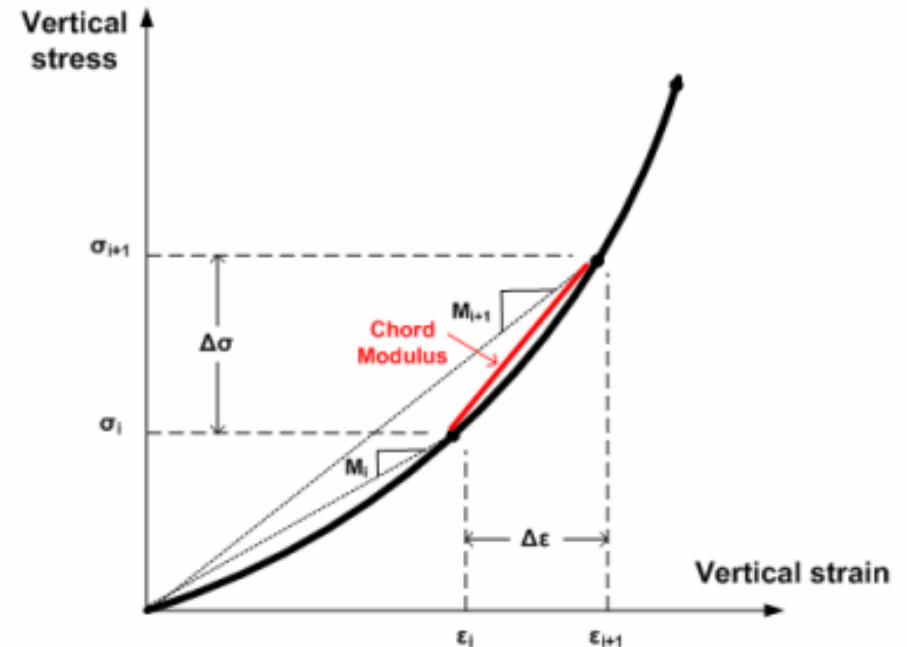
- **Soil Model**
 - **Simple**
 - **Linear Elastic Soil**
 - **Intermediate**
 - **Overburden Dependent**
 - **Complex**
 - **Duncan / Duncan - Selig Soil**
 - **Extended Harden**

- **Structural Backfill Limits**
 - **Width on both side of culvert walls**
 - **Height above the top slab**



(3 Input Parameter)

- **Soil Model**
 - **Simple**
 - **Linear Elastic Soil**
 - **Intermediate**
 - **Overburden Dependent**
 - **Complex**
 - **Duncan / Duncan - Selig Soil**
 - **Extended Harden**
- **Structural Backfill Limits**
 - **Width on both side of culvert walls**
 - **Height above the top slab**



(4 Input Parameter)

➤ Soil Model

➤ Simple

- Linear Elastic Soil

➤ Intermediate

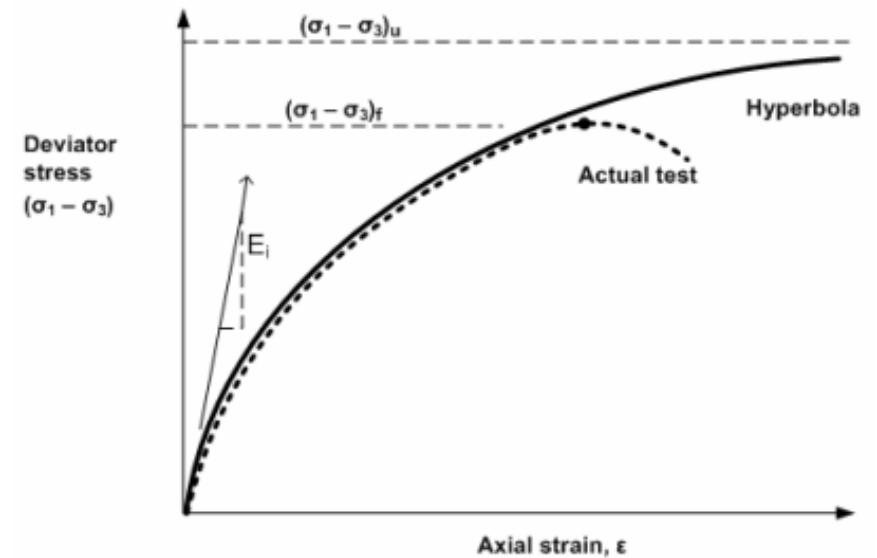
- Overburden Dependent

➤ Complex

- Duncan / Duncan - Selig Soil
- Extended Harden

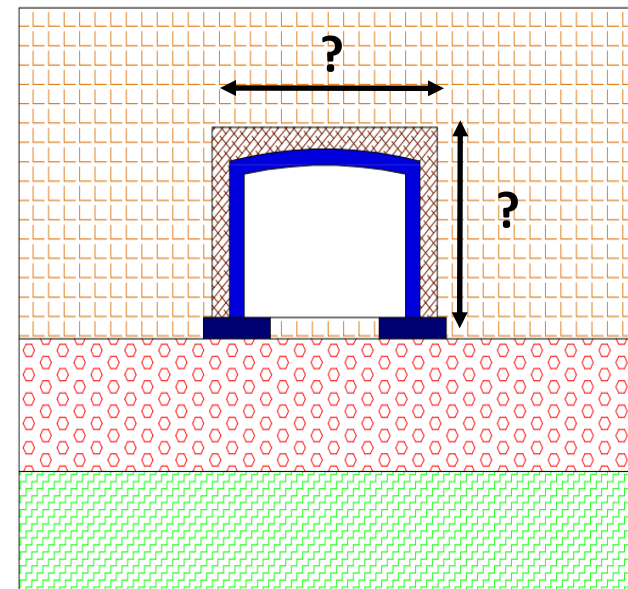
➤ Structural Backfill Limits

- Width on both side of culvert walls
- Height above the top slab



(12 Input Parameter)

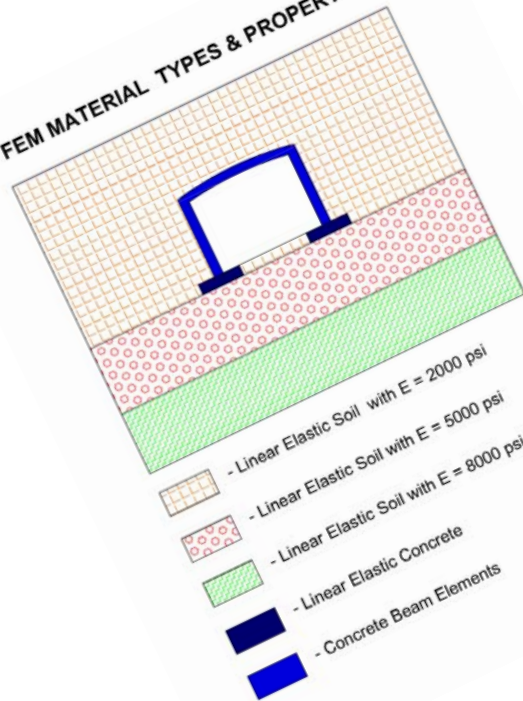
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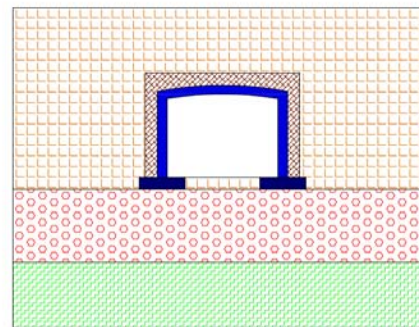
PARAMETRIC STUDY

10 Different finite element models are considered to identify critical soil parameters

FEM MATERIAL TYPES & PROPERTIES

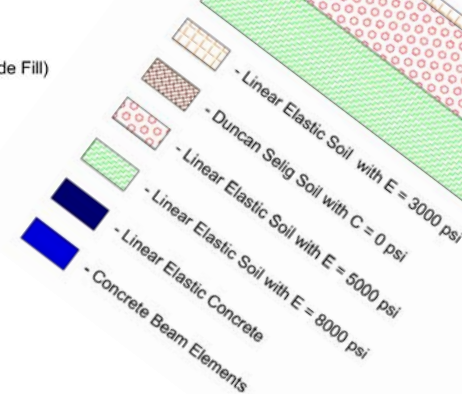


FEM MATERIAL TYPES & PROPERTIES



- Linear Elastic Soil with E = 3000 psi
- Duncan Selig Soil with C = 0 psi (2ft Side Fill)
- Linear Elastic Soil with E = 5000 psi
- Linear Elastic Soil with E = 8000 psi
- Linear Elastic Concrete
- Concrete Beam Elements

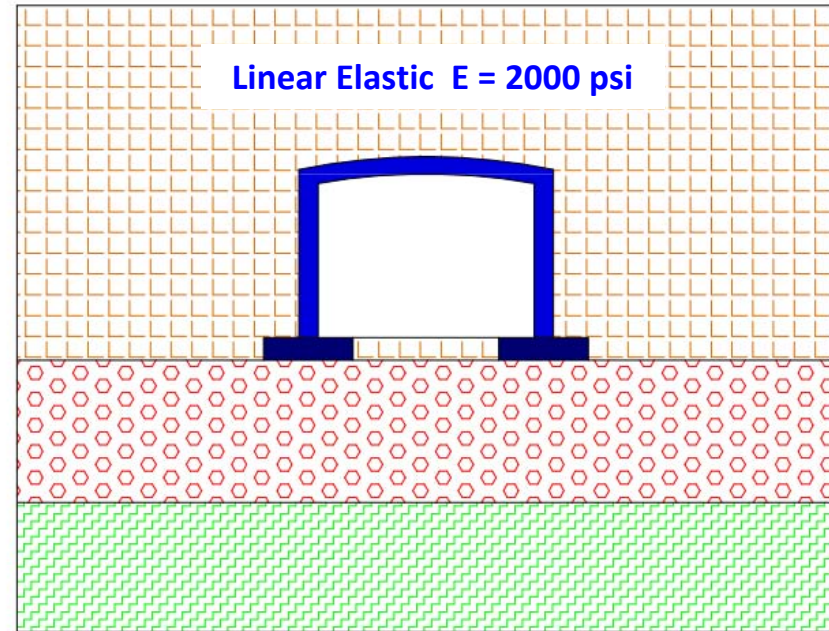
FEM MATERIAL TYPES & PROPERTIES




FEM MATERIAL TYPES & PROPERTIES

FINITE ELEMENT MODEL - 1

- **In-Situ Soil assigned with zero density (Affects trench condition analysis)**
- **Structural Backfill assigned with zero cohesion to meet Caltrans backfill specifications**
- **Final Model shall not be overly conservative, but design should include possible uncertainties**



 - Linear Elastic Soil with E = 2000 psi

 - Linear Elastic Soil with E = 5000 psi

 - Linear Elastic Soil with E = 8000 psi

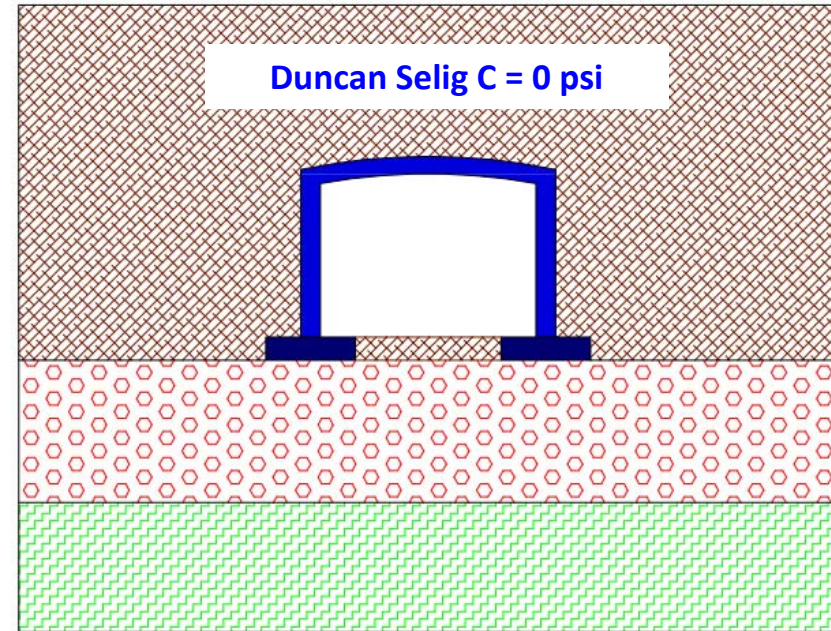
 - Linear Elastic Concrete

 - Concrete Beam Elements

FEM MATERIAL TYPES & PROPERTIES

FINITE ELEMENT MODEL - 2

- **In-Situ Soil assigned with zero density (Affects trench condition analysis)**
- **Structural Backfill assigned with zero cohesion to meet Caltrans backfill specifications**
- **Final Model shall not be overly conservative, but design should include possible uncertainties**



- Duncan Selig Soil with C = 0 psi



- Linear Elastic Soil with E = 5000 psi



- Linear Elastic Soil with E = 8000 psi



- Linear Elastic Concrete

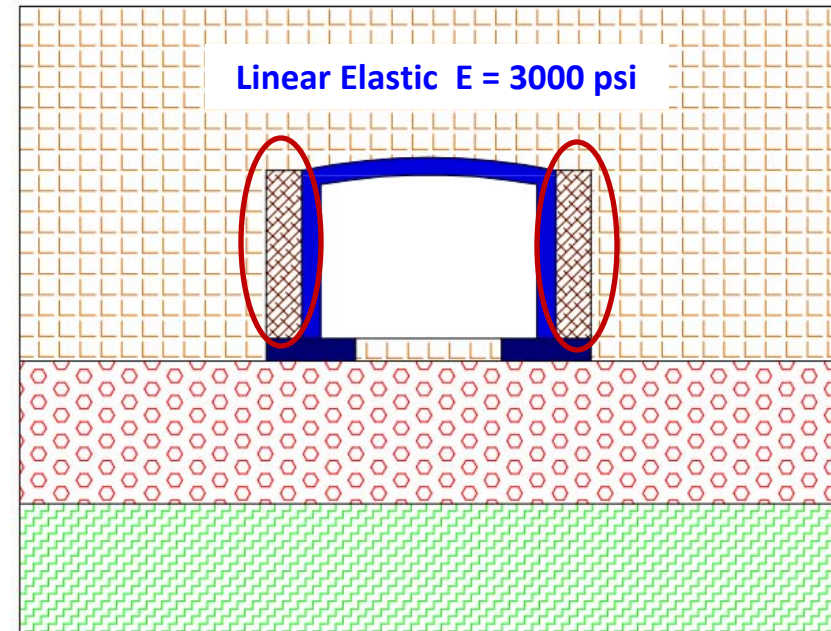


- Concrete Beam Elements

FEM MATERIAL TYPES & PROPERTIES

FINITE ELEMENT MODEL - 3

- **In-Situ Soil assigned with zero density (Affects trench condition analysis)**
- **Structural Backfill assigned with zero cohesion to meet Caltrans backfill specifications**
- **Final Model shall not be overly conservative, but design should include possible uncertainties**




 - Linear Elastic Soil with $E = 3000$ psi

 - Duncan Selig Soil with $C = 0$ psi

 - Linear Elastic Soil with $E = 5000$ psi

 - Linear Elastic Soil with $E = 8000$ psi

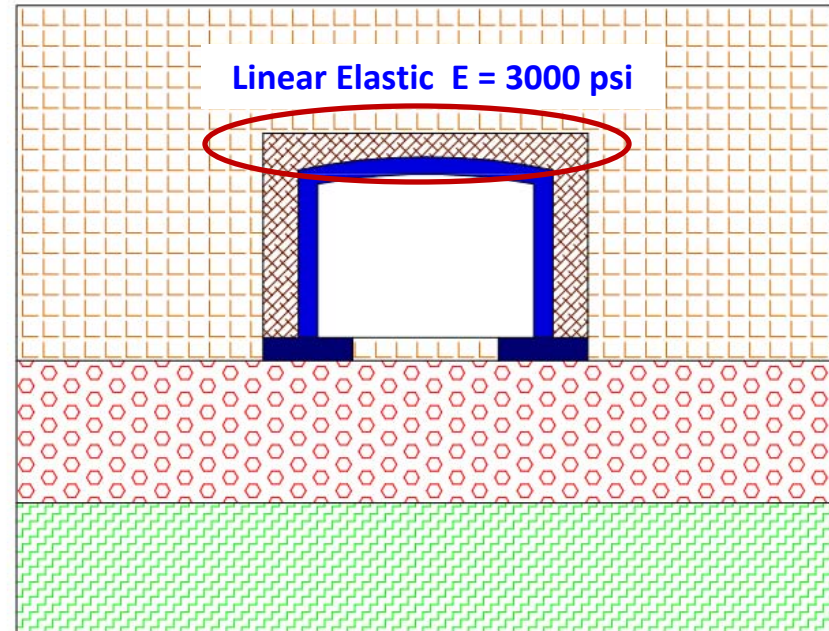
 - Linear Elastic Concrete

 - Concrete Beam Elements

FEM MATERIAL TYPES & PROPERTIES

FINITE ELEMENT MODEL - 4

- **In-Situ Soil assigned with zero density (Affects trench condition analysis)**
- **Structural Backfill assigned with zero cohesion to meet Caltrans backfill specifications**
- **Final Model shall not be overly conservative, but design should include possible uncertainties**



 - Linear Elastic Soil with $E = 3000$ psi

 - Duncan Selig Soil with $C = 0$ psi

 - Linear Elastic Soil with $E = 5000$ psi

 - Linear Elastic Soil with $E = 8000$ psi

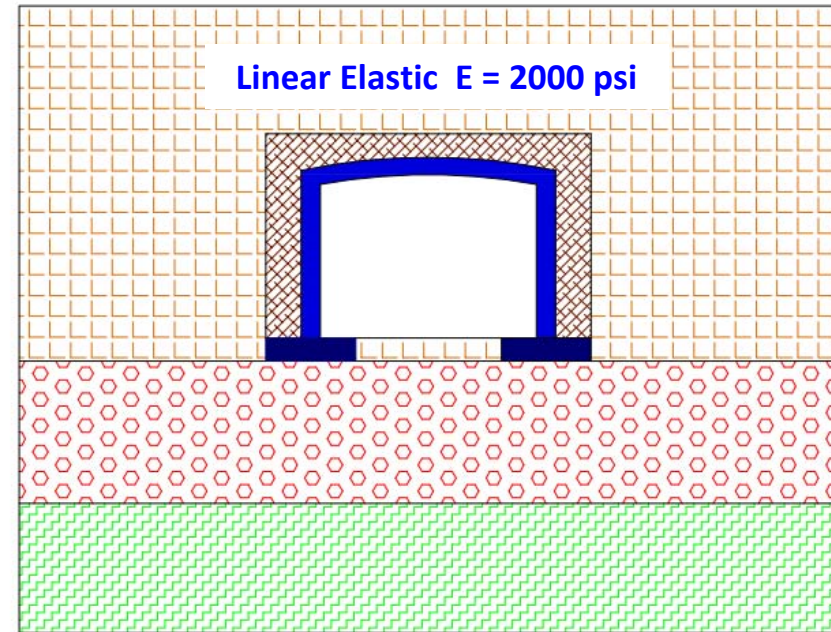
 - Linear Elastic Concrete

 - Concrete Beam Elements

FEM MATERIAL TYPES & PROPERTIES

FINITE ELEMENT MODEL - 5

- **In-Situ Soil assigned with zero density (Affects trench condition analysis)**
- **Structural Backfill assigned with zero cohesion to meet Caltrans backfill specifications**
- **Final Model shall not be overly conservative, but design should include possible uncertainties**




 - Linear Elastic Soil with $E = 2000$ psi

 - Duncan Selig Soil with $C = 0$ psi

 - Linear Elastic Soil with $E = 5000$ psi

 - Linear Elastic Soil with $E = 8000$ psi

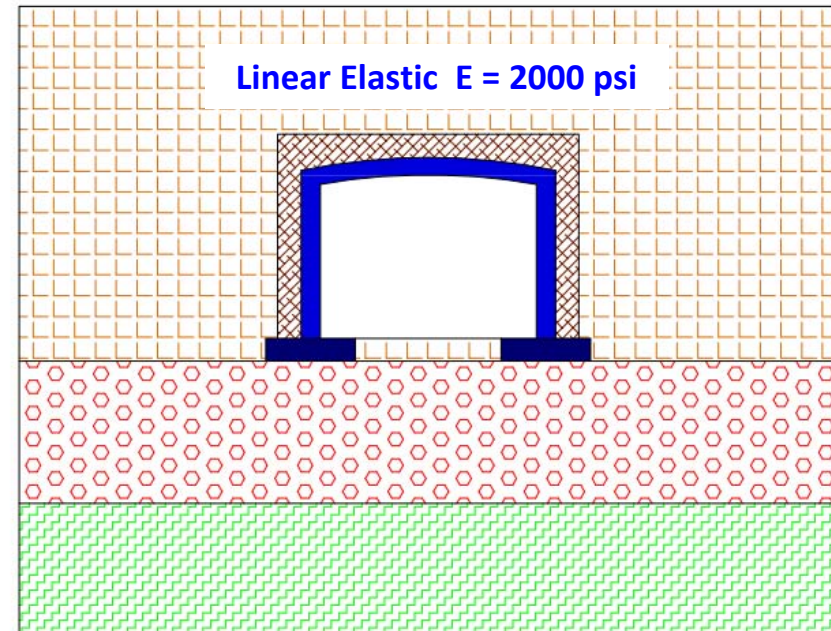
 - Linear Elastic Concrete


 - Concrete Beam Elements

FEM MATERIAL TYPES & PROPERTIES

FINITE ELEMENT MODEL - 6

- **In-Situ Soil assigned with zero density (Affects trench condition analysis)**
- **Structural Backfill assigned with zero cohesion to meet Caltrans backfill specifications**
- **Final Model shall not be overly conservative, but design should include possible uncertainties**



 - Linear Elastic Soil with $E = 2000$ psi

 - Duncan Selig Soil with $C = 0$ psi (2ft Side Fill)

 - Linear Elastic Soil with $E = 5000$ psi

 - Linear Elastic Soil with $E = 8000$ psi

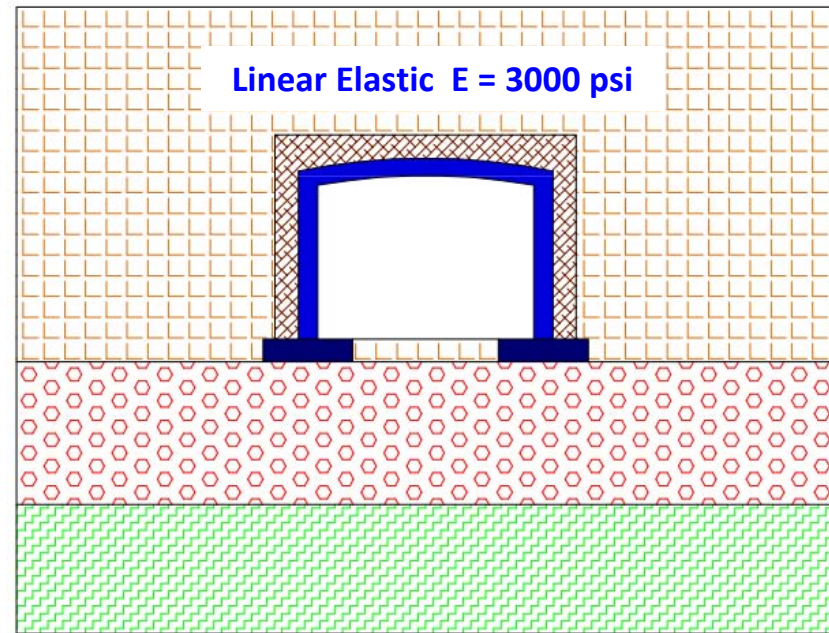
 - Linear Elastic Concrete







 - Concrete Beam Elements

FEM MATERIAL TYPES & PROPERTIES

FINITE ELEMENT MODEL - 7

- **In-Situ Soil assigned with zero density (Affects trench condition analysis)**
- **Structural Backfill assigned with zero cohesion to meet Caltrans backfill specifications**
- **Final Model shall not be overly conservative, but design should include possible uncertainties**

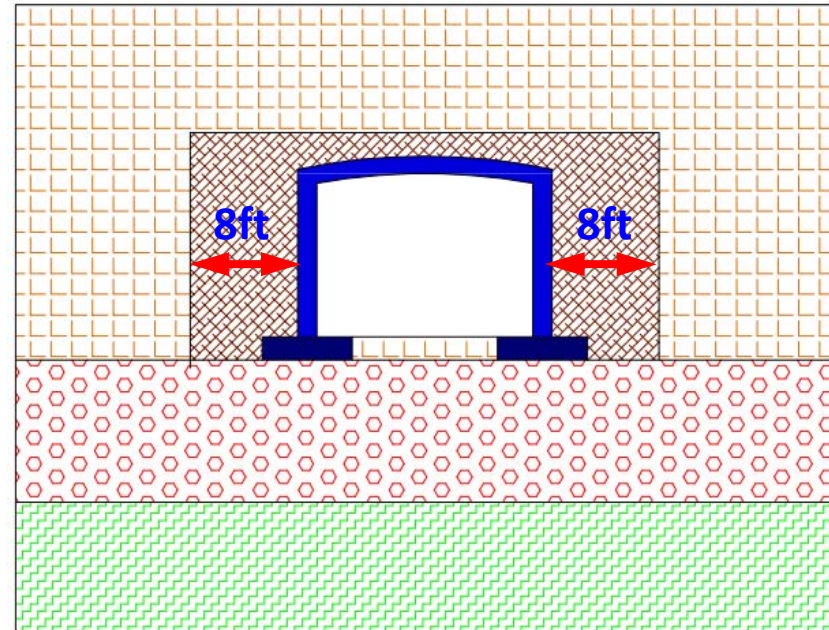


-  - Linear Elastic Soil with $E = 3000$ psi
-  - Duncan Selig Soil with $C = 0$ psi (2ft Side Fill)
-  - Linear Elastic Soil with $E = 5000$ psi
-  - Linear Elastic Soil with $E = 8000$ psi
-  - Linear Elastic Concrete
-  - Concrete Beam Elements

FINITE ELEMENT MODEL - 8

- **In-Situ Soil assigned with zero density (Affects trench condition analysis)**
- **Structural Backfill assigned with zero cohesion to meet Caltrans backfill specifications**
- **Final Model shall not be overly conservative, but design should include possible uncertainties**

FEM MATERIAL TYPES & PROPERTIES



 - Linear Elastic Soil with $E = 3000$ psi

 - Duncan Selig Soil with $C = 0$ psi

 - Linear Elastic Soil with $E = 5000$ psi

 - Linear Elastic Soil with $E = 8000$ psi

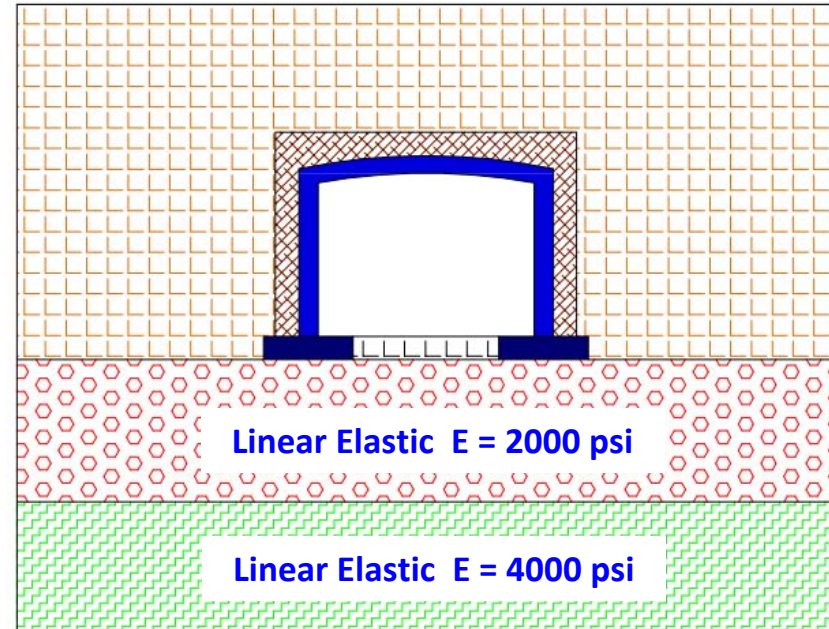
 - Linear Elastic Concrete







 - Concrete Beam Elements

FEM MATERIAL TYPES & PROPERTIES

FINITE ELEMENT MODEL - 9

- **In-Situ Soil assigned with zero density (Affects trench condition analysis)**
- **Structural Backfill assigned with zero cohesion to meet Caltrans backfill specifications**
- **Final Model shall not be overly conservative, but design should include possible uncertainties**

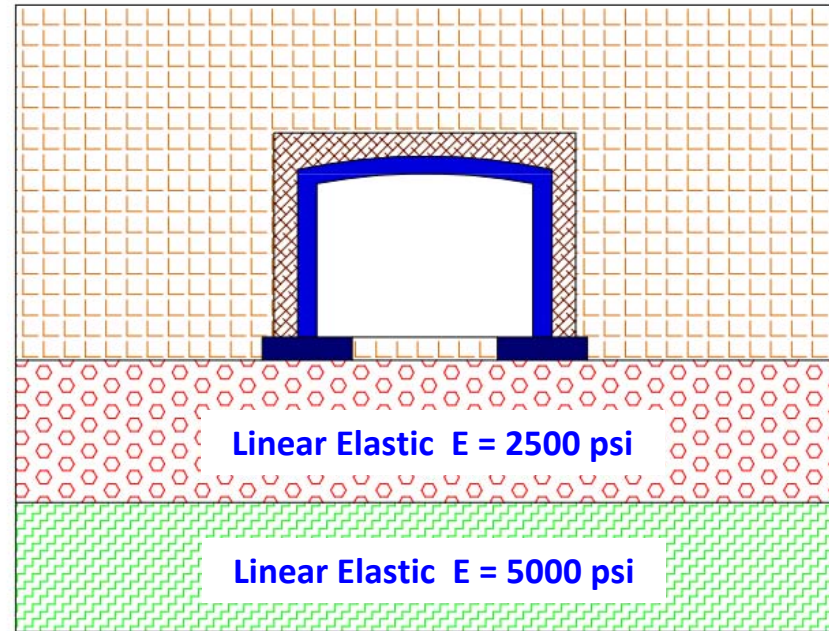




-  - Linear Elastic Soil with E = 2000 psi
-  - Duncan Selig Soil with C = 0 psi (2ft Side Fill)
-  - Linear Elastic Soil with E = 2000 psi
-  - Linear Elastic Soil with E = 4000 psi
-  - Linear Elastic Concrete
-  - Concrete Beam Elements



FEM MATERIAL TYPES & PROPERTIES



FINITE ELEMENT MODEL - 10

- **In-Situ Soil assigned with zero density (Affects trench condition analysis)**
- **Structural Backfill assigned with zero cohesion to meet Caltrans backfill specifications**
- **Final Model shall not be overly conservative, but design should include possible uncertainties**

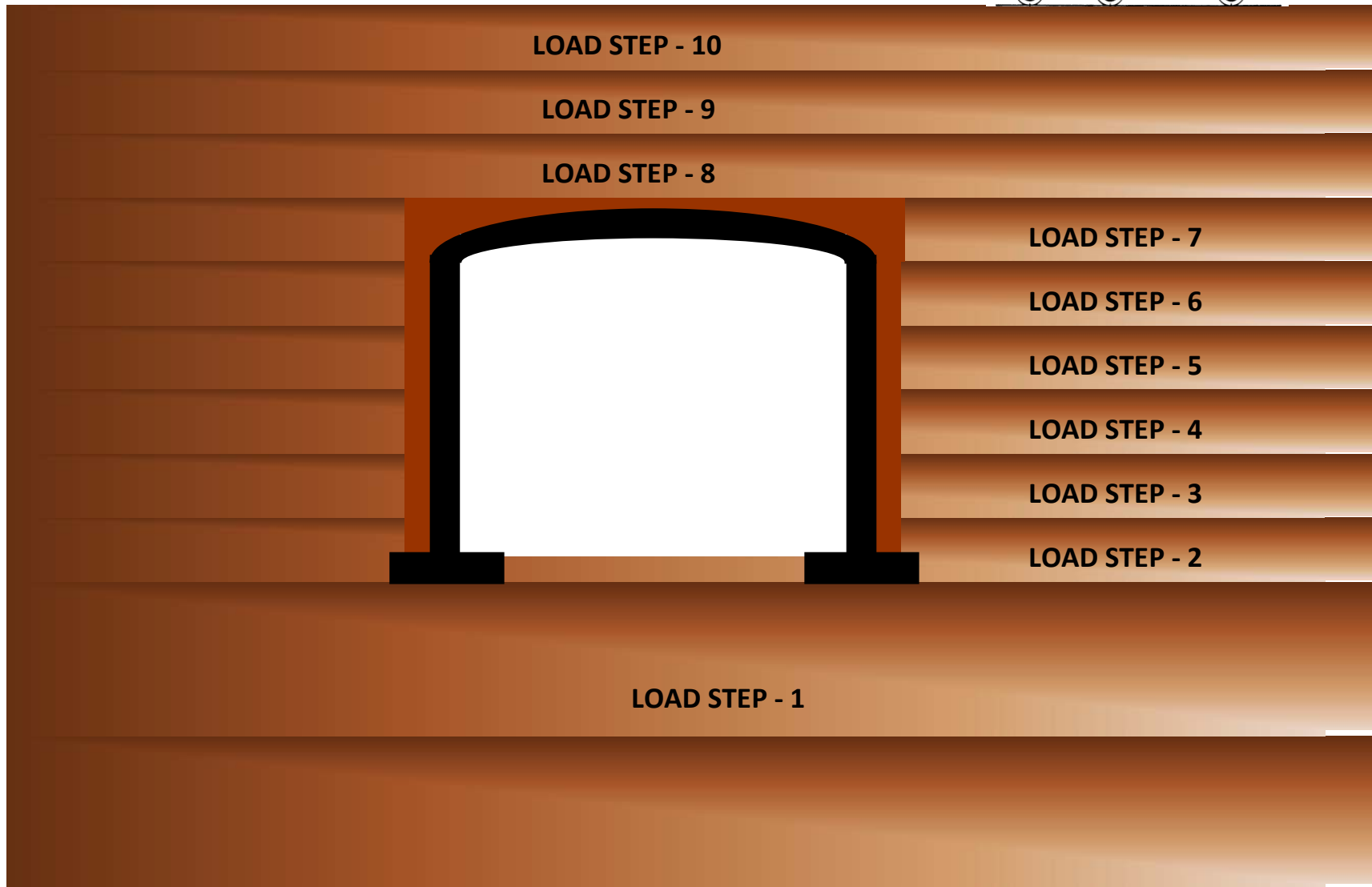
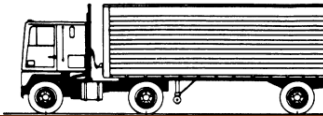


-  - Linear Elastic Soil with $E = 2000$ psi
-  - Duncan Selig Soil with $C = 0$ psi (2ft Side Fill)

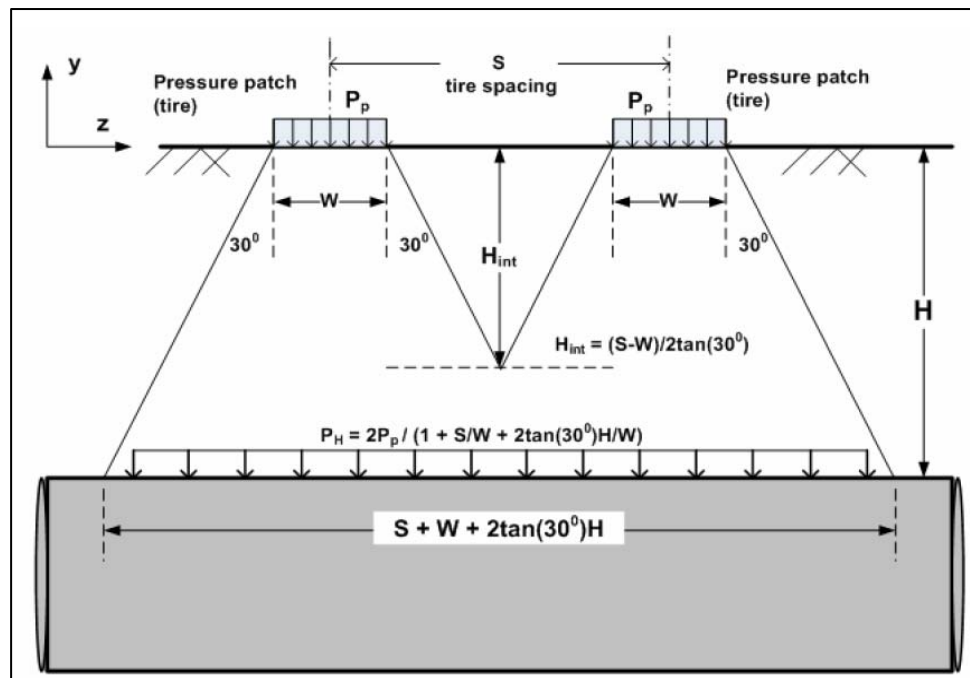
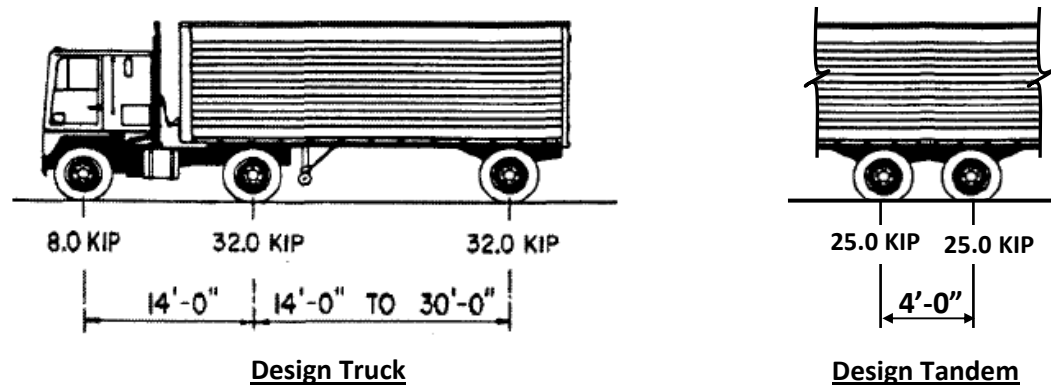
-  - Linear Elastic Soil with $E = 2500$ psi
-  - Linear Elastic Soil with $E = 5000$ psi

-  - Linear Elastic Concrete
-  - Concrete Beam Elements

BACKFILL SEQUENCE/LOAD STEPS



LIVE LOAD ON CULVERTS



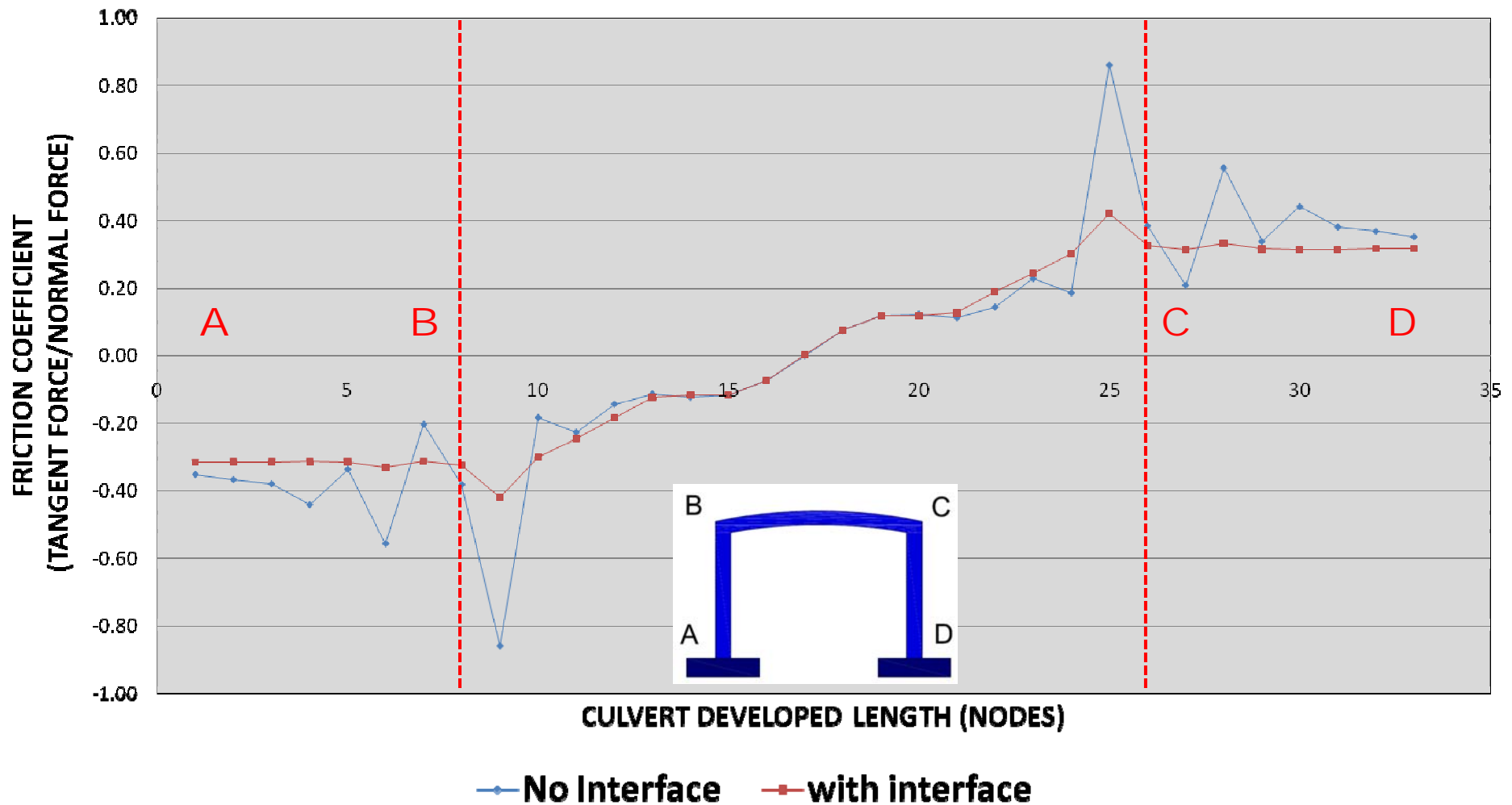
AASHTO LRFD two-wheel load distribution along axis of culvert. CANDE 2007 Solution Method Figure 8.1.3-1

- **COMBINATION-1: Critical for culvert corner (EH-Max + EV-Max)**
- **COMBINATION-2: Critical for wall span moment (EH-Max + EV-Min)**
- **COMBINATION-3: Critical for culvert top slab (EH-Min + EV-Max)**
- **COMBINATION-4: Service load Combination for Crack Control**

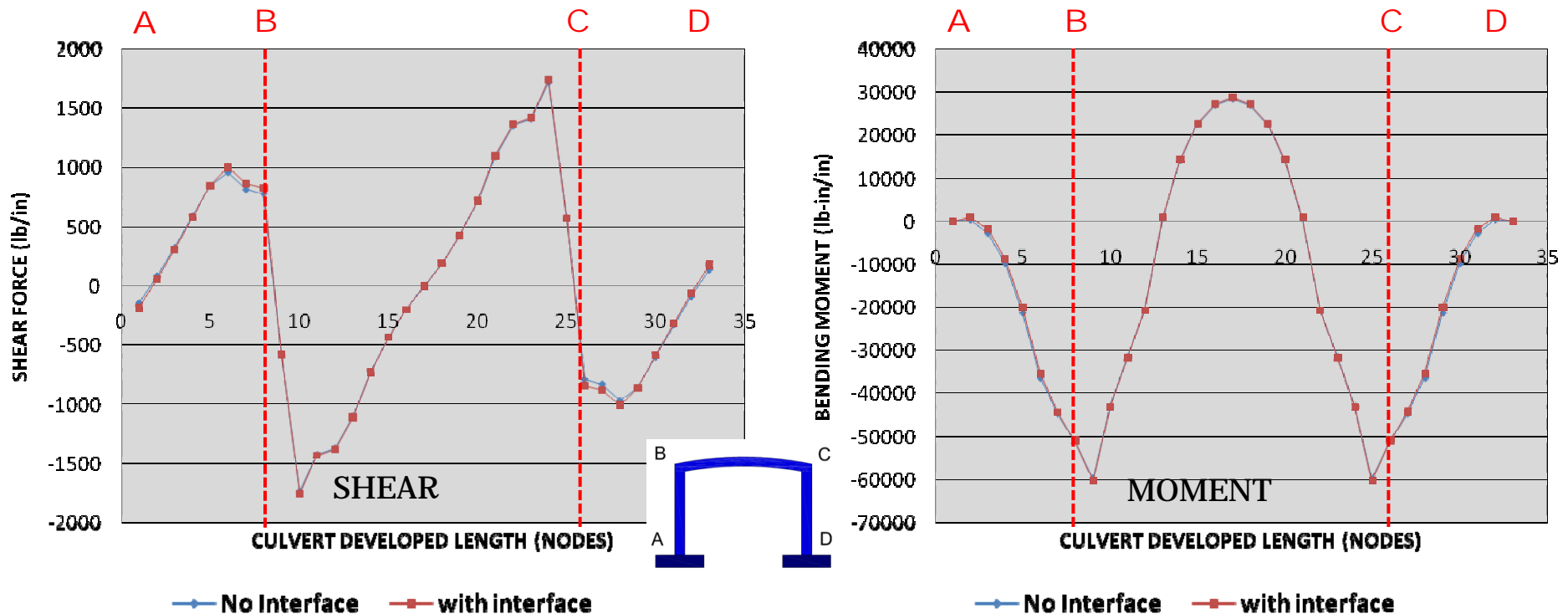
LOAD STEPS	COMB-1	COMB-2	COMB-3	COMB-4
Load Step – 1 (For In-Situ Soil)	0	0	0	0
Load Step – 2 - 5 (For Side Soil) - EH	1.5	1.5	0.9	1.0
Load Step – 5 (For Soil over top slab) - EV	1.3	1.0	1.3	1.0
Load Step- 12-XX (Live Load) - LL	1.75	0	1.75	1.0

INTERFACE ELEMENTS

- **Types: Fully Bonded/ Partially Bonded/ Frictionless**
- **Transfer normal & shear forces based on friction coefficient value of element**



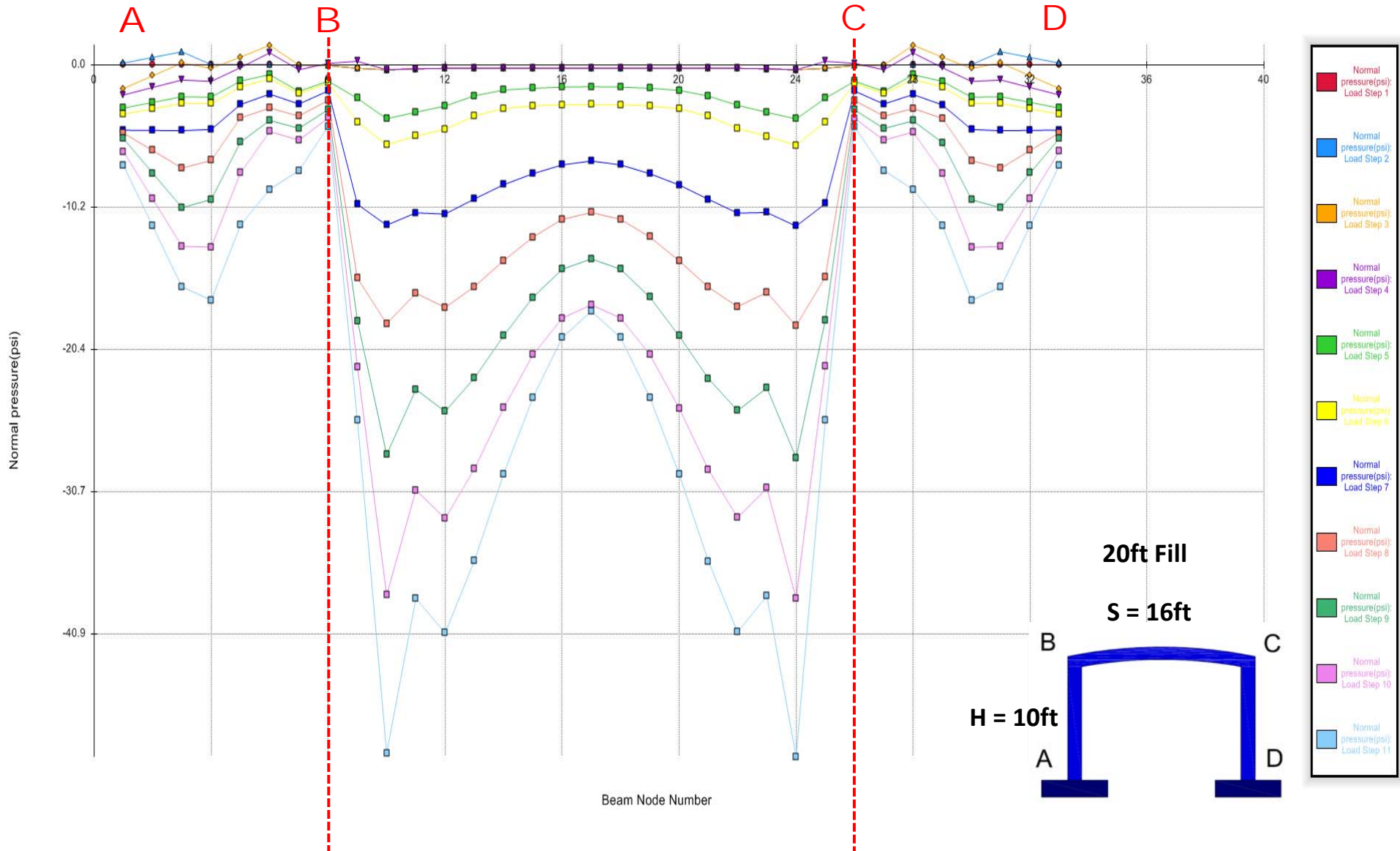
INTERFACE VS NO INTERFACE



- **Model with interface elements produces more realistic results**
- **Accuracy gained appears to be very minor and does not justify the additional effort required**

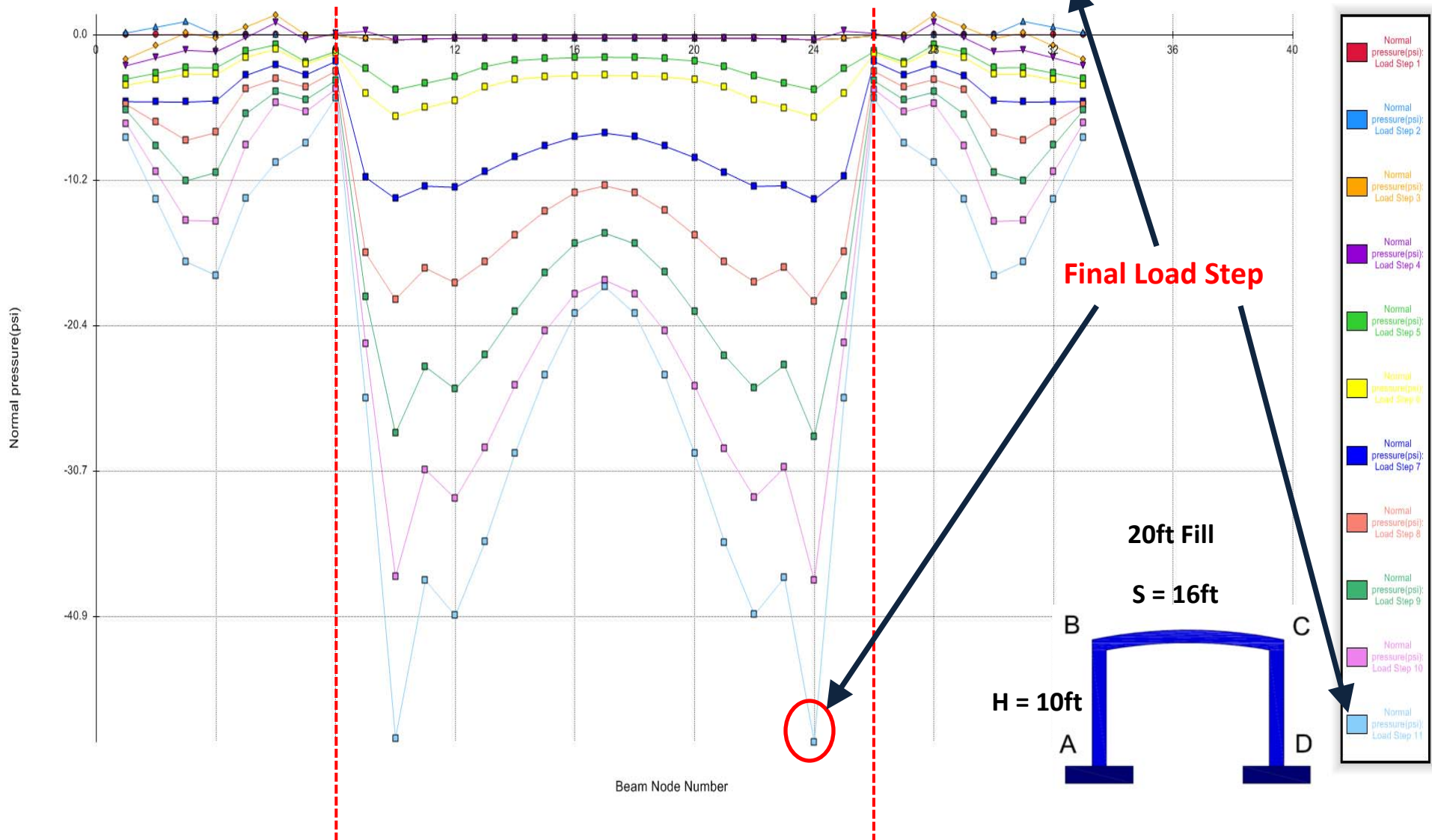
SAMPLE RESULT OUTPUT

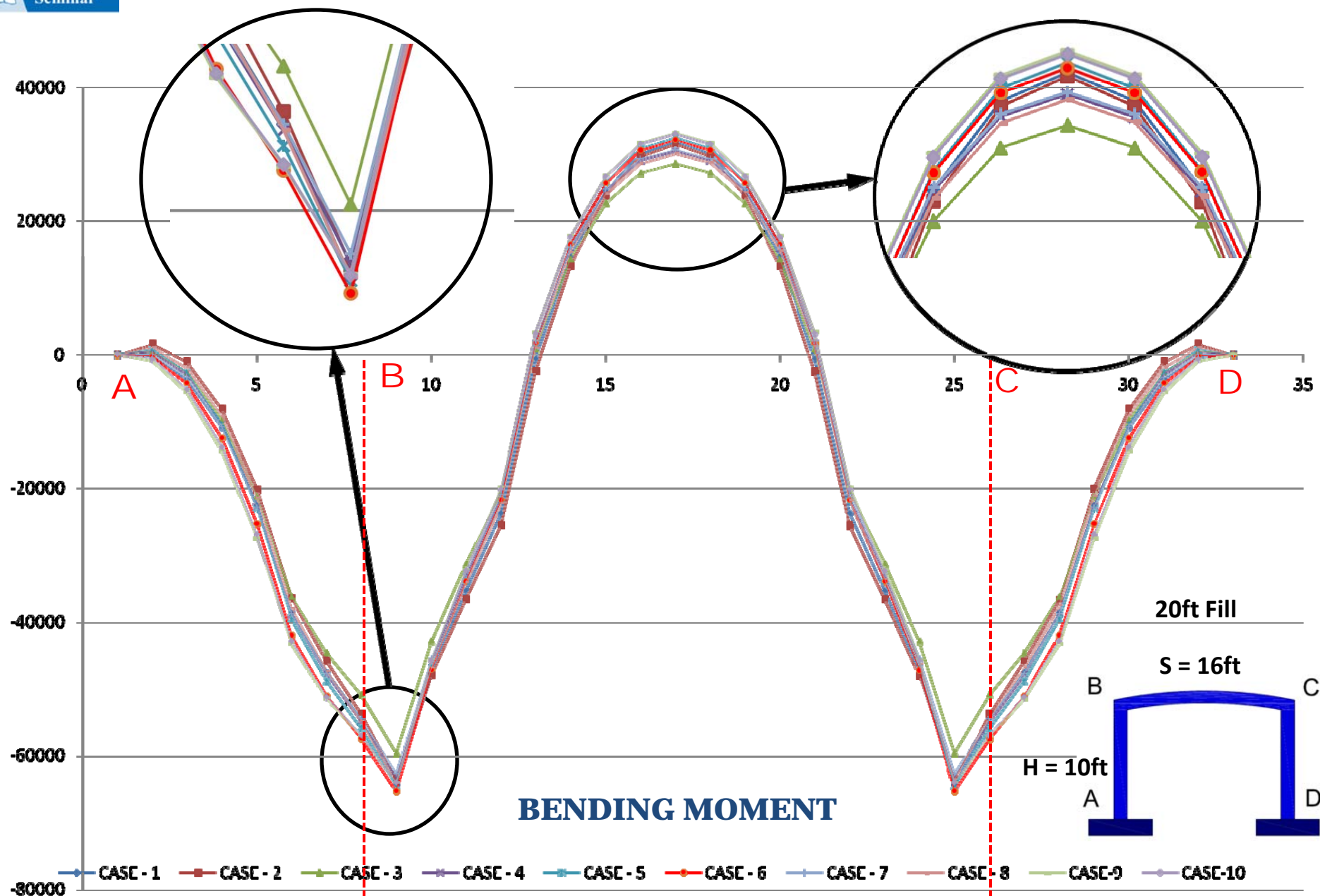
Normal pressure(psi): Load steps 1,2,3,4,5,6,7,8,9,10,11,

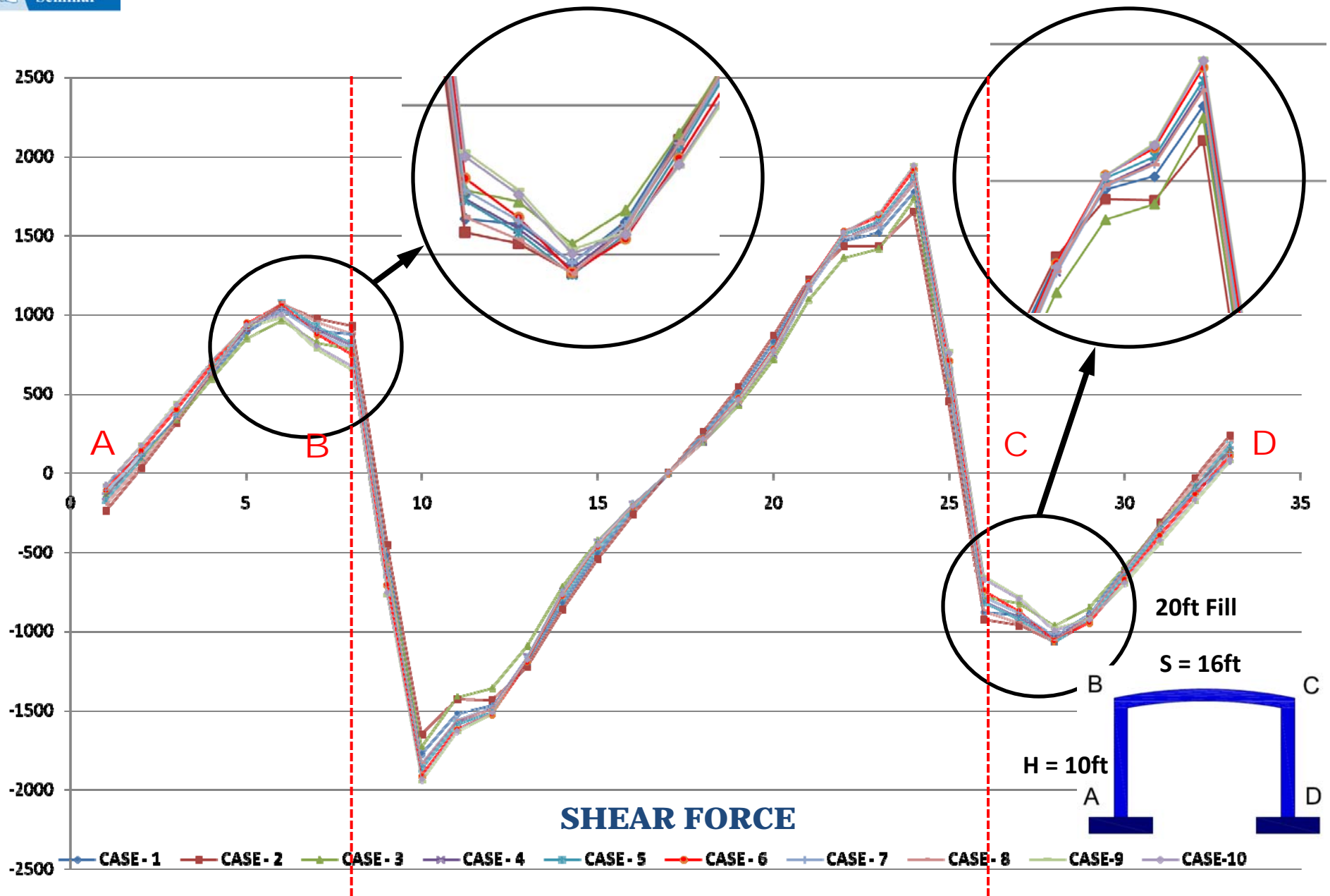


SAMPLE RESULT OUTPUT

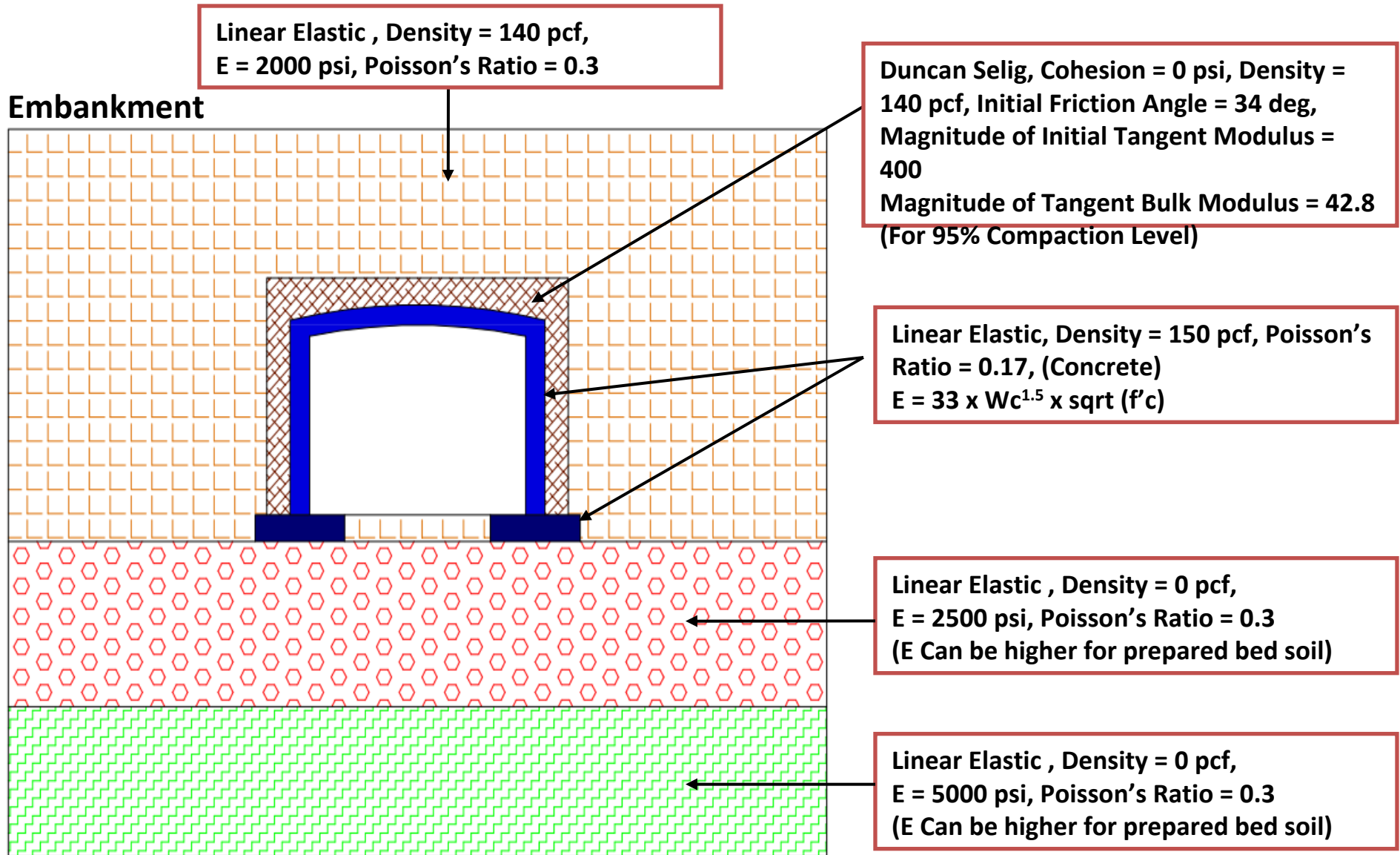
Normal pressure(psi): Load steps 1,2,3,4,5,6,7,8,9,10,11,



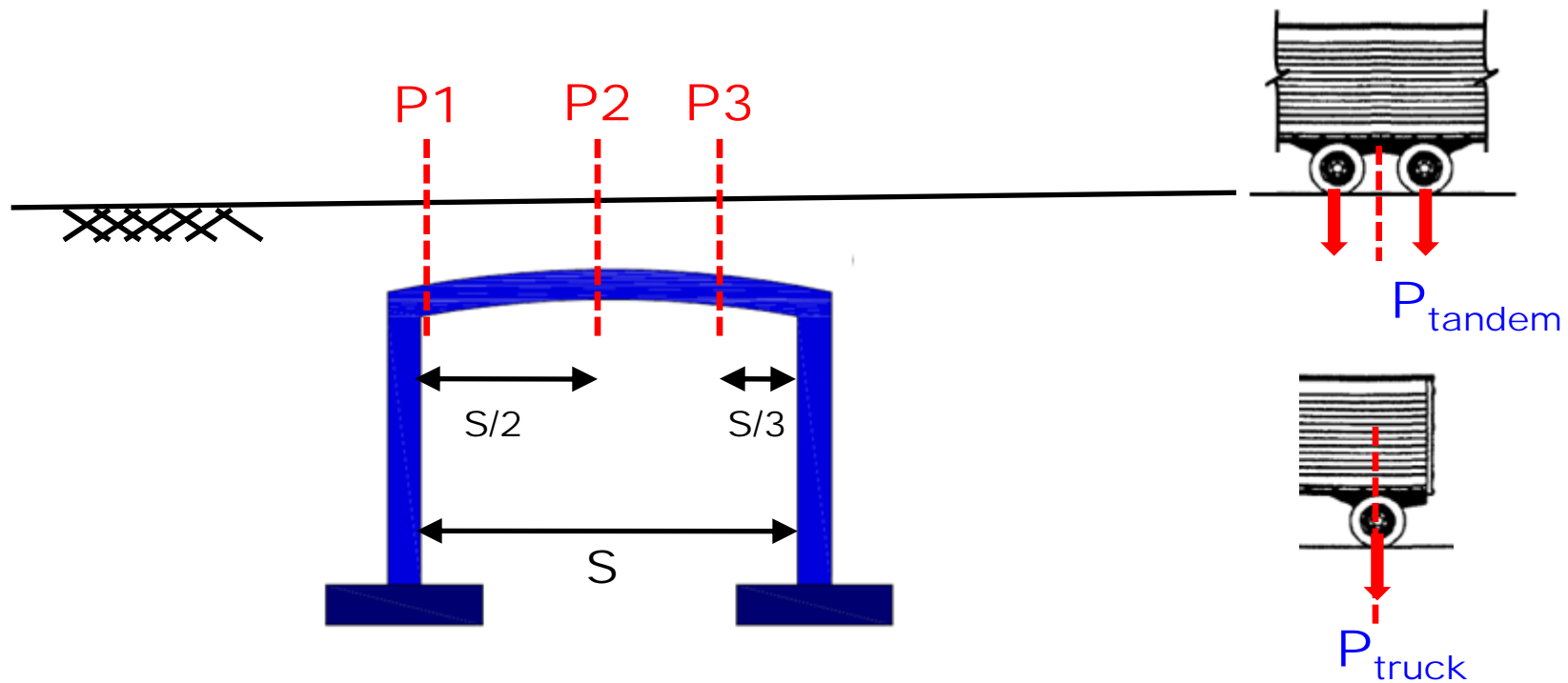




RECOMMENDED MODEL

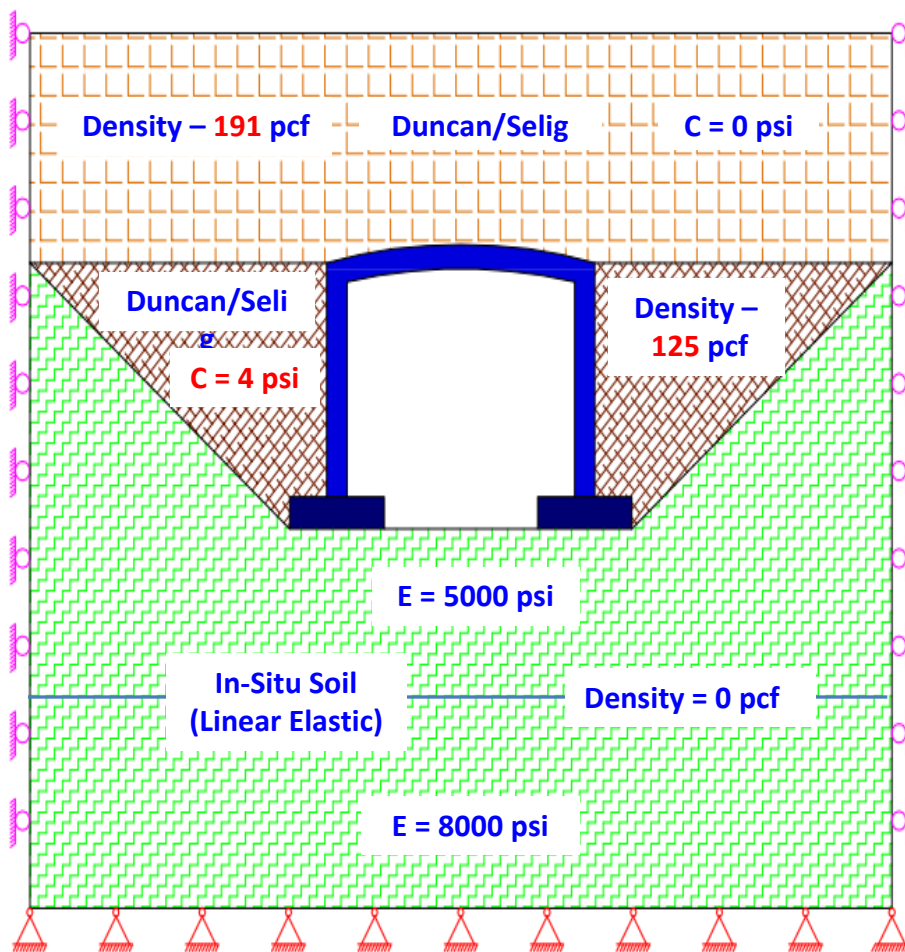


RECOMENDED MINIMUM LIVE LOAD APPLICATION



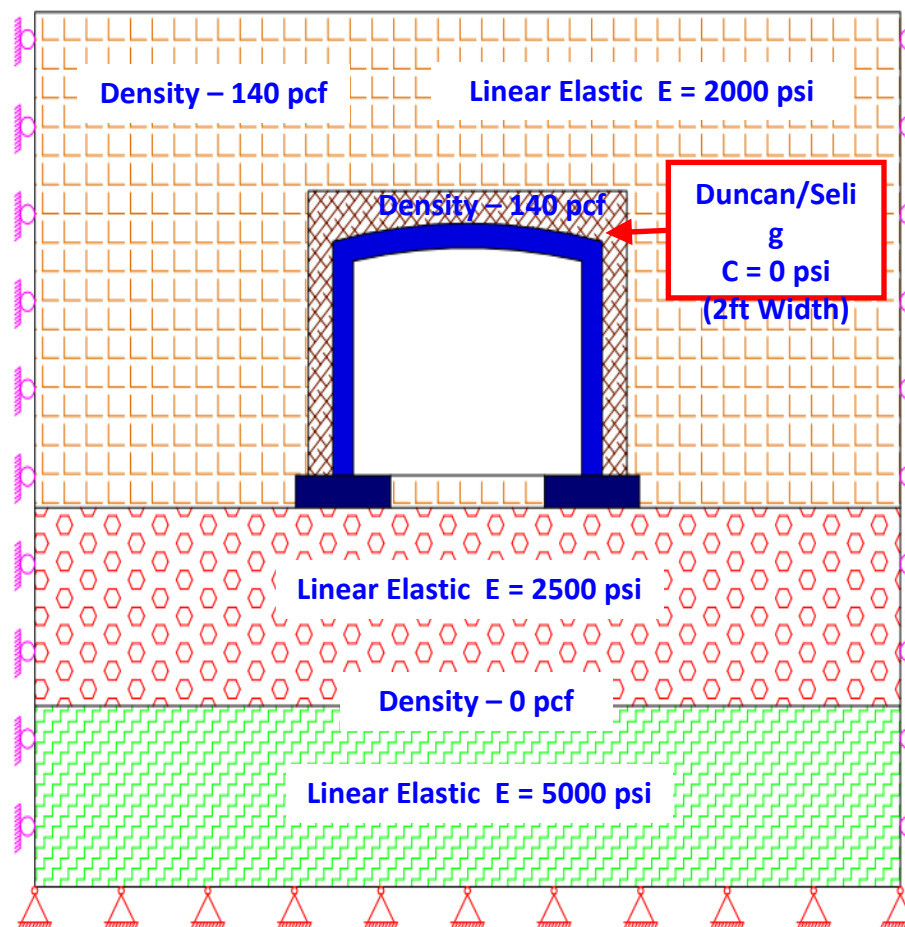
LOCATION	CRITICAL EFFECTS
P1	Shear in Top Slab
P2	Maximum Top Slab Span Moment
P3	Maximum Culvert Corner Moment

Trench Condition



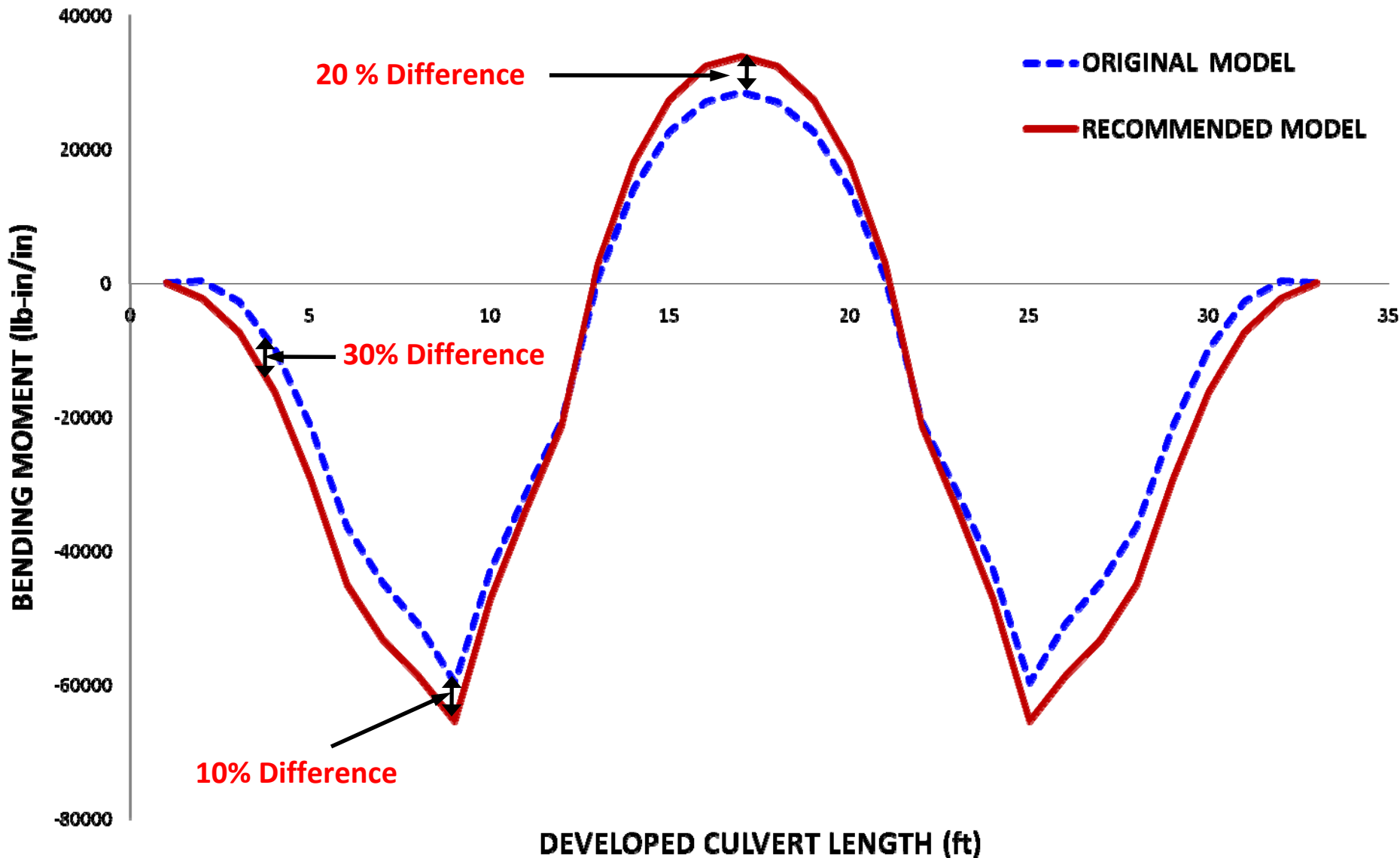
**ORIGINAL MODEL
(REVIEW PROBLEM)**

Embankment Condition



RECOMMENDED MODEL

ORIGINAL MODEL VS RECOMENDED MODEL



FOR LOAD COMBINATION -1

Finite Element Based LRFD Design of Bottomless Culverts

Thank You

Q & A

E-mail :

Ahmad.Abdel-Karim@aecom.com

Craig.Chatelain@aecom.com

Bob.Fish@aecom.com

Ahilan.Selladurai@aecom.com